

# Simulation of Brightness Temperatures for the Microwave Radiometer (MWR) on the Aquarius/SAC-D Mission

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Understanding  
the Interaction  
Between Ocean  
Circulation, the  
Water Cycle,  
and Climate by  
**Measuring  
Ocean Salinity**

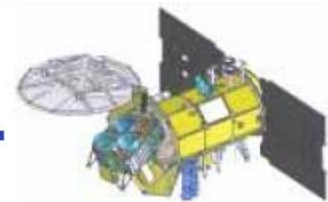
# Outline

- Thesis Objective
- Aquarius Salinity Measurements
- Aquarius Radiometer/Scatterometer
- Microwave Radiometer (MWR)
- MWR  $T_b$  Simulation Requirements
- Yaw Steering Analysis
- Post-Launch Inter-Satellite Radiometric Calibration using WindSat

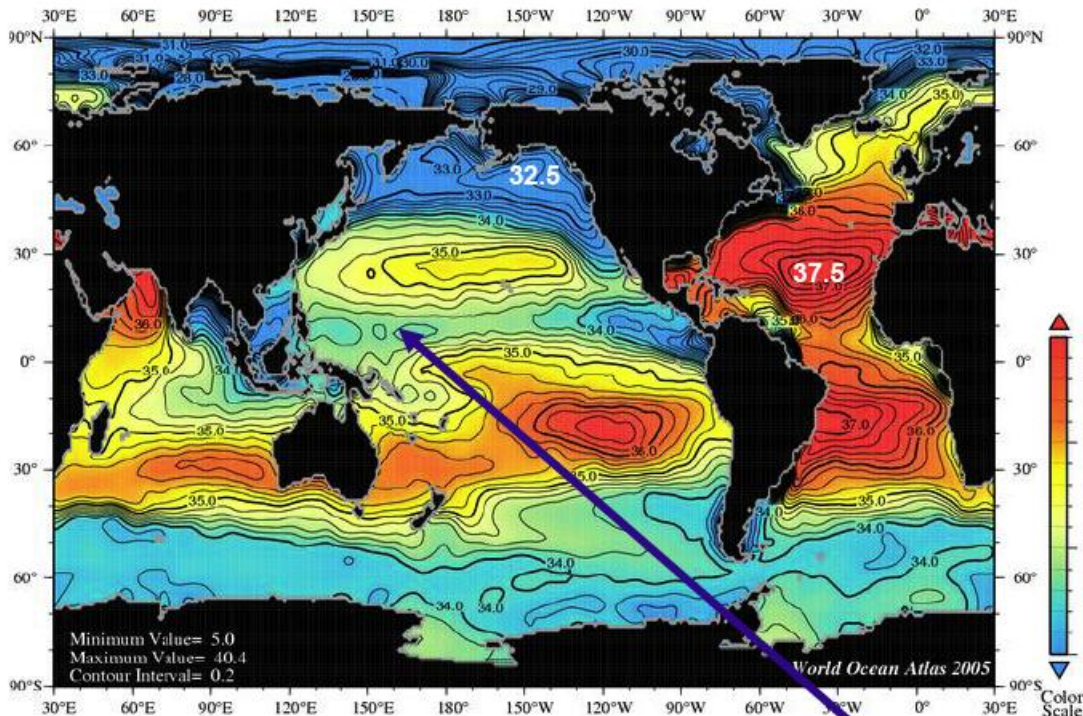
# Thesis Objective

- Simulate realistic ocean brightness temperatures ( $T_b$ ) for the 3-channel Microwave Radiometer (MWR) on Aquarius/SAC-D
  - To be used by CONAE for pre-launch geophysical retrieval algorithms development
- Evaluate the proposed MWR measurement geometry and verify the requirements for spatial/temporal sampling
- Perform a preliminary study for the post-launch inter-satellite radiometric calibration using the WindSat radiometer as a reference





Annual salinity [PSS] at the surface.



Mean Ocean SSS Dynamic Range is ~5 psu (32.5 to 37.5 open ocean)

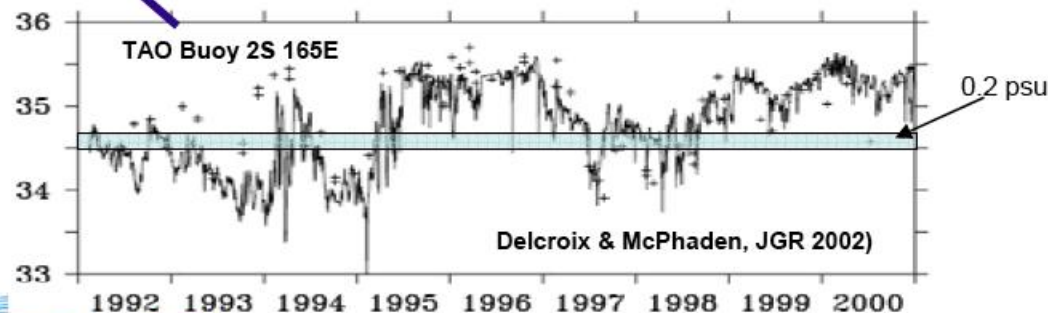
0.2 psu accuracy yields ~25:1 signal/error relative to mean field

Accuracy and signal/error improves with averaging interval (Table)

Random Error Reduction with Averaging Interval						
	Instantaneous	7 Days	28 Days	90 Days	1 Year	3 Years
Global RMS (psu)	0.87	0.33	0.20	0.09	0.05	0.03
Mean Signal/Error	6	15	25	55	110	190

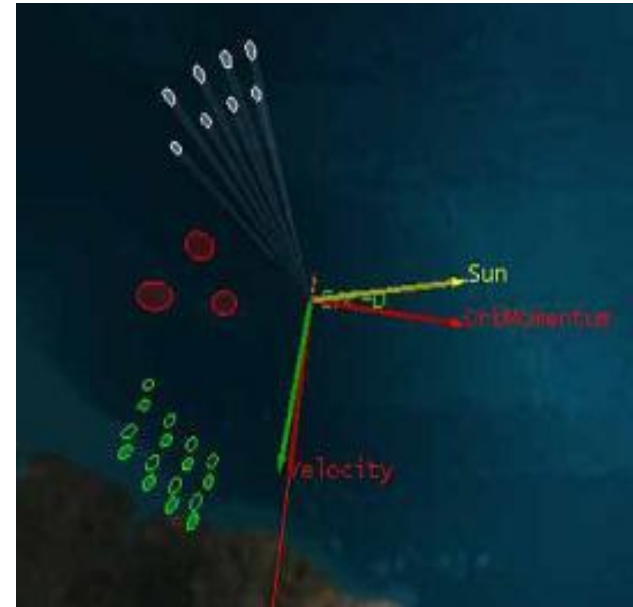
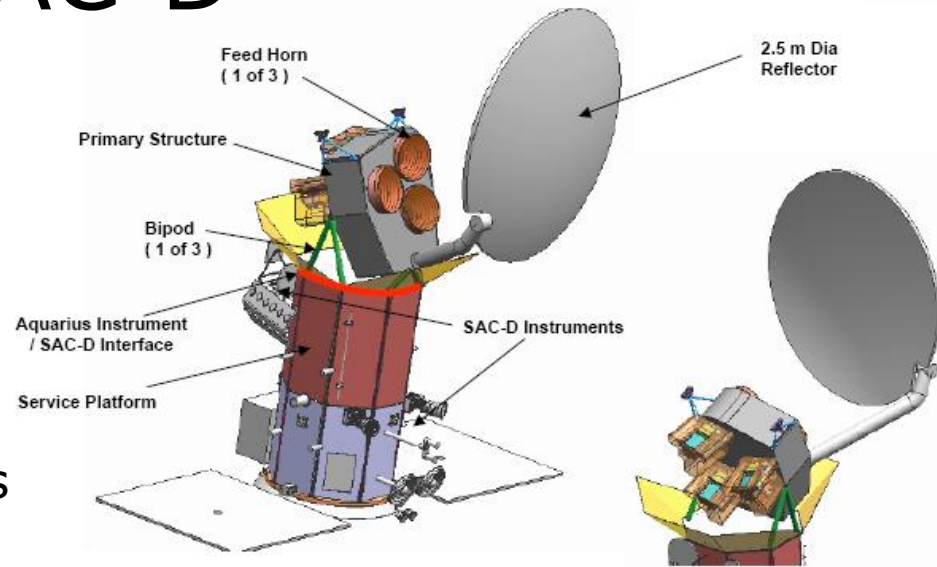
- Climatology maps based on the available historical data are interpolated over ~1000 km scales due to data sparseness.
- Aquarius' 150 km resolution will provide almost an order of magnitude improvement

- Interannual SSS variability range is ~2 psu in the western tropical Pacific
- 0.2 psu monthly accuracy is at the detection limit of short time scales, and easily resolves the interannual signals related to El Niño



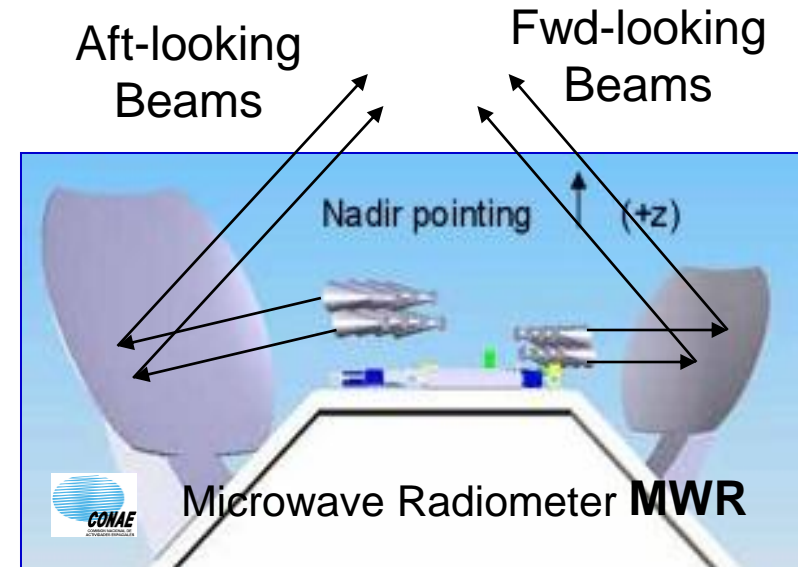
# Aquarius Radiometer/Scatterometer on SAC-D

- Antenna
  - Radiometer & Scatterometer share feeds and 2.5 m reflector
  - Three footprints in pushbroom configuration
- Radiometer
  - 1.413 GHz V, H-pol & 3rd Stokes
- Scatterometer
  - 1.26 GHz H-pol
  - Provides a critical correction for surface roughness
- Beams
  - Inner – 76 x 94 Km
  - Middle – 84 x 120 Km
  - Outer – 96 x 156 Km

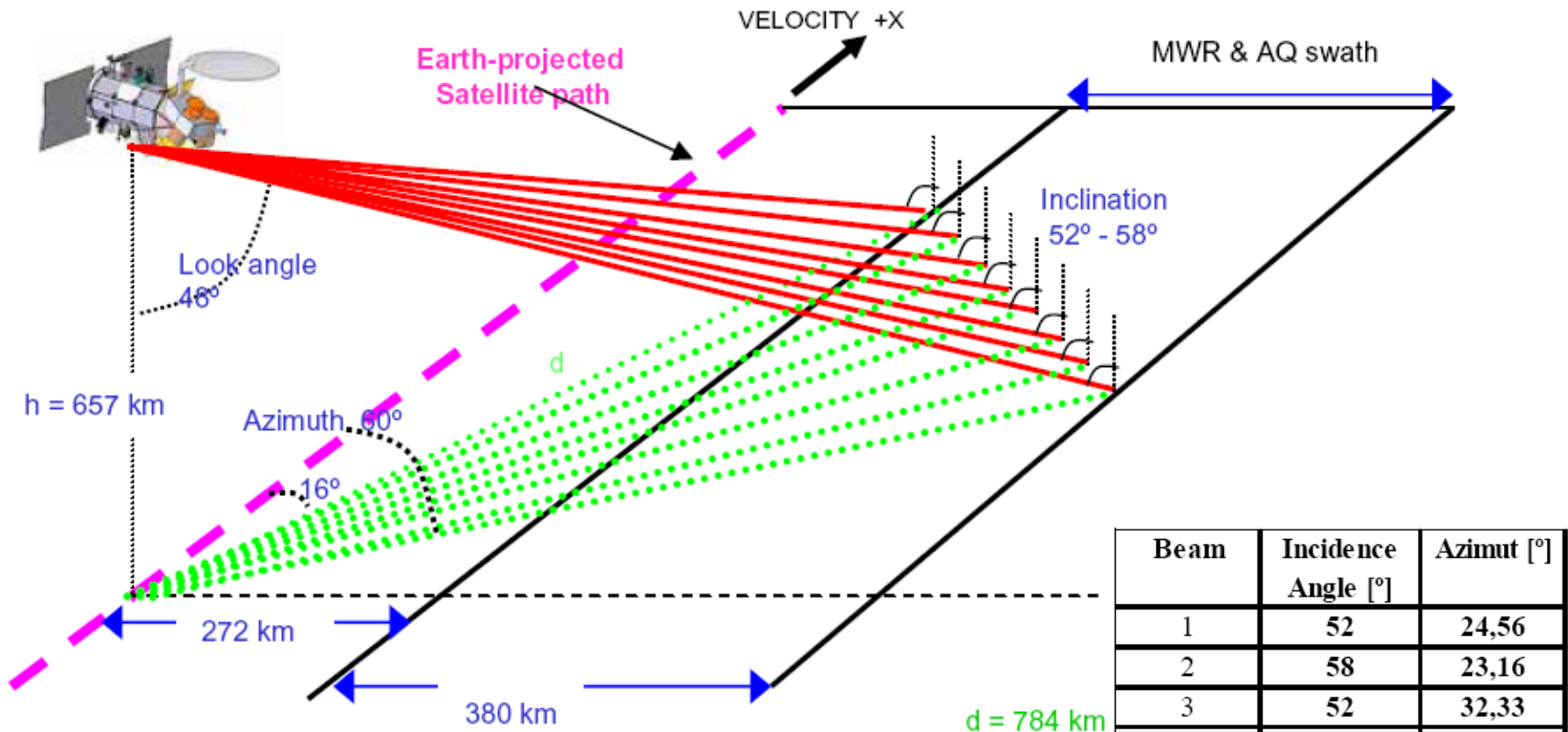


# Microwave Radiometer (MWR) on SAC-D

- Radiometer
  - Two radiometers
    - 23.8 GHz (K band, V-pol)
    - 36.5 GHz (Ka band, H, V-pol, +45° & -45° polarized output)
    - All the polarizations are measured simultaneously
- Antenna
  - Two Multi-beam parabolic-torus reflectors
    - Forward & Aft looking beams
    - 8 beams in push-broom configuration
    - Two incidence angles, 52° & 58°
    - IFOV Resolution of  $\sim 40$  km



# MWR Forward Beam (Ka-Band) Geometry

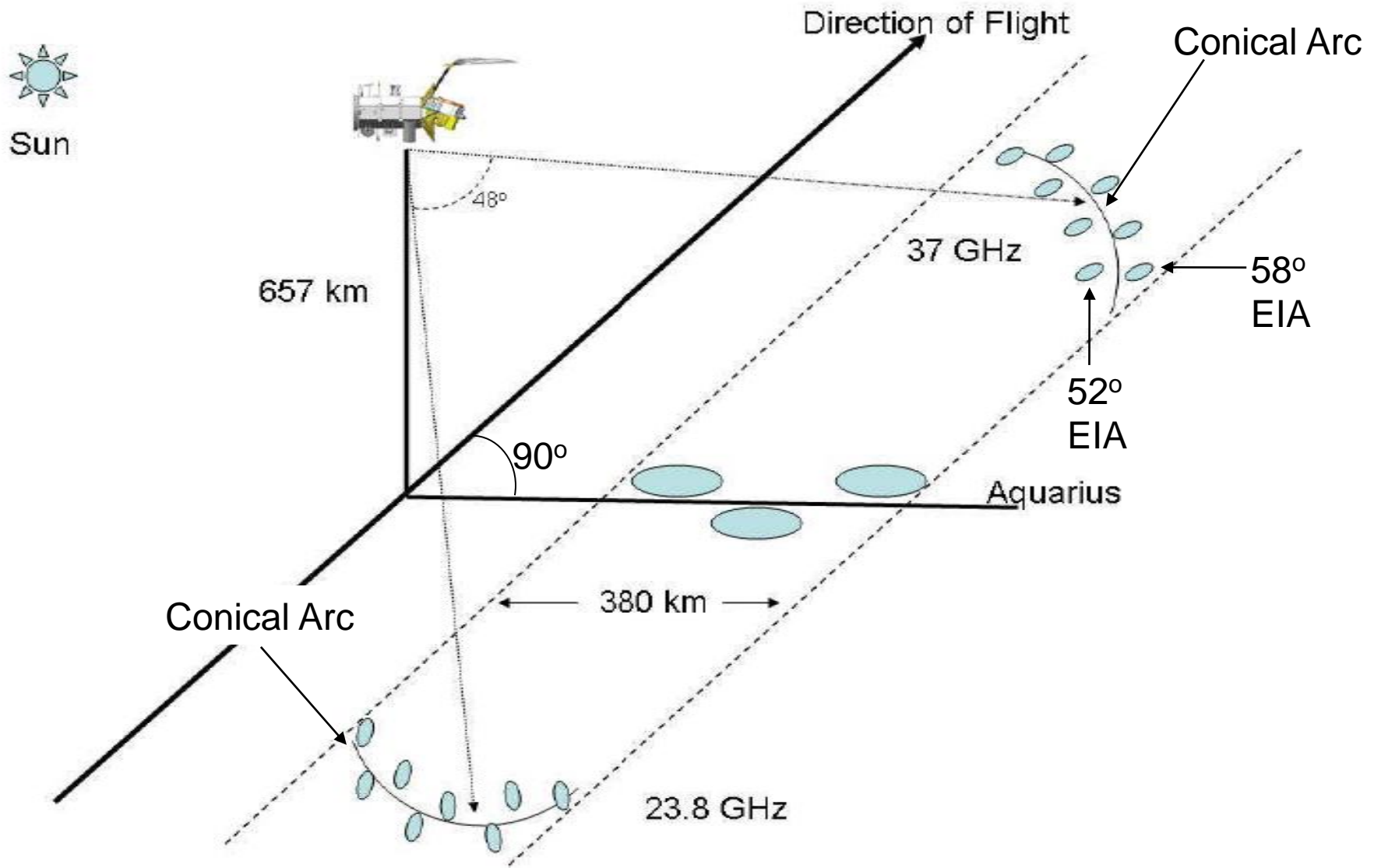


Beam	Incidence Angle [°]	Azimuth [°]
1	52	24,56
2	58	23,16
3	52	32,33
4	58	29,56
5	52	41,44
6	58	37,12
7	52	52,97
8	58	46,13

- Satellite's velocity along +X
- Only forward beams are shown
- Four beams @  $52^\circ$  & four @  $58^\circ$  EIA, alternating

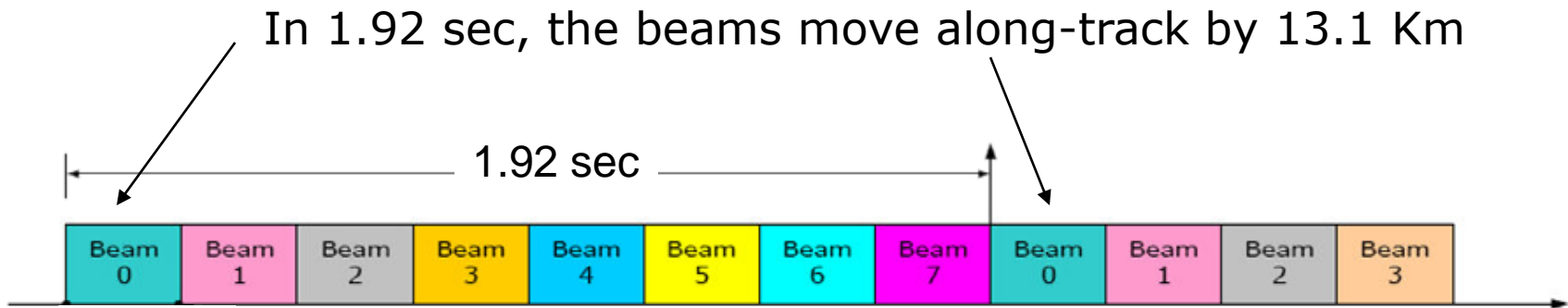


# MWR Fwd & Aft Beam Geometry





# MWR beams are sequentially sampled in time



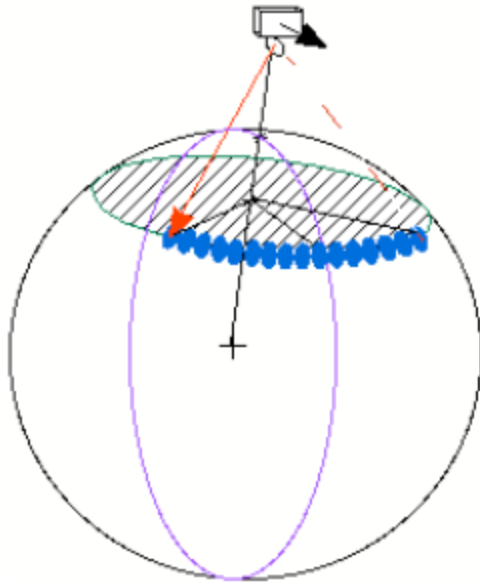
- The sampling time made the simulation very challenging since the beams are sampled sequentially at 0.24 sec intervals in which the spacecraft (and hence the footprint) moves as well

# MWR $T_b$ Simulation Requirements

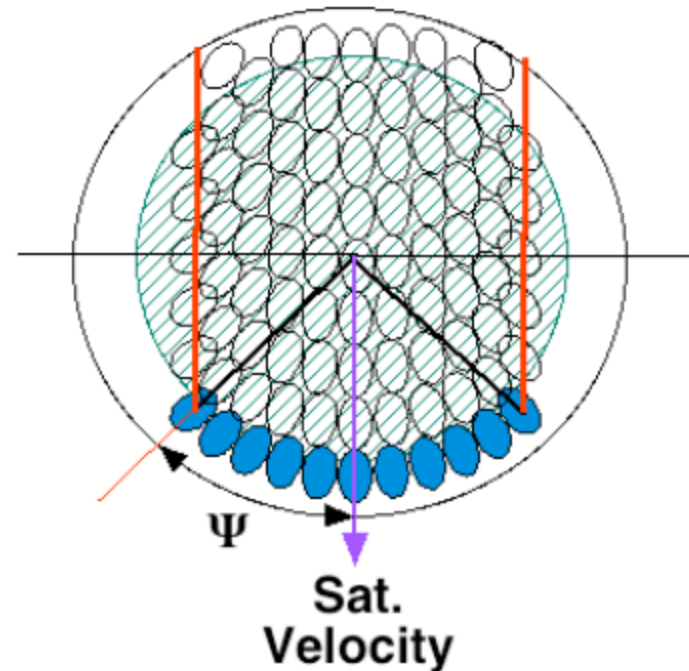


# Conical Scanning Sensor Geometry

## 3-D View



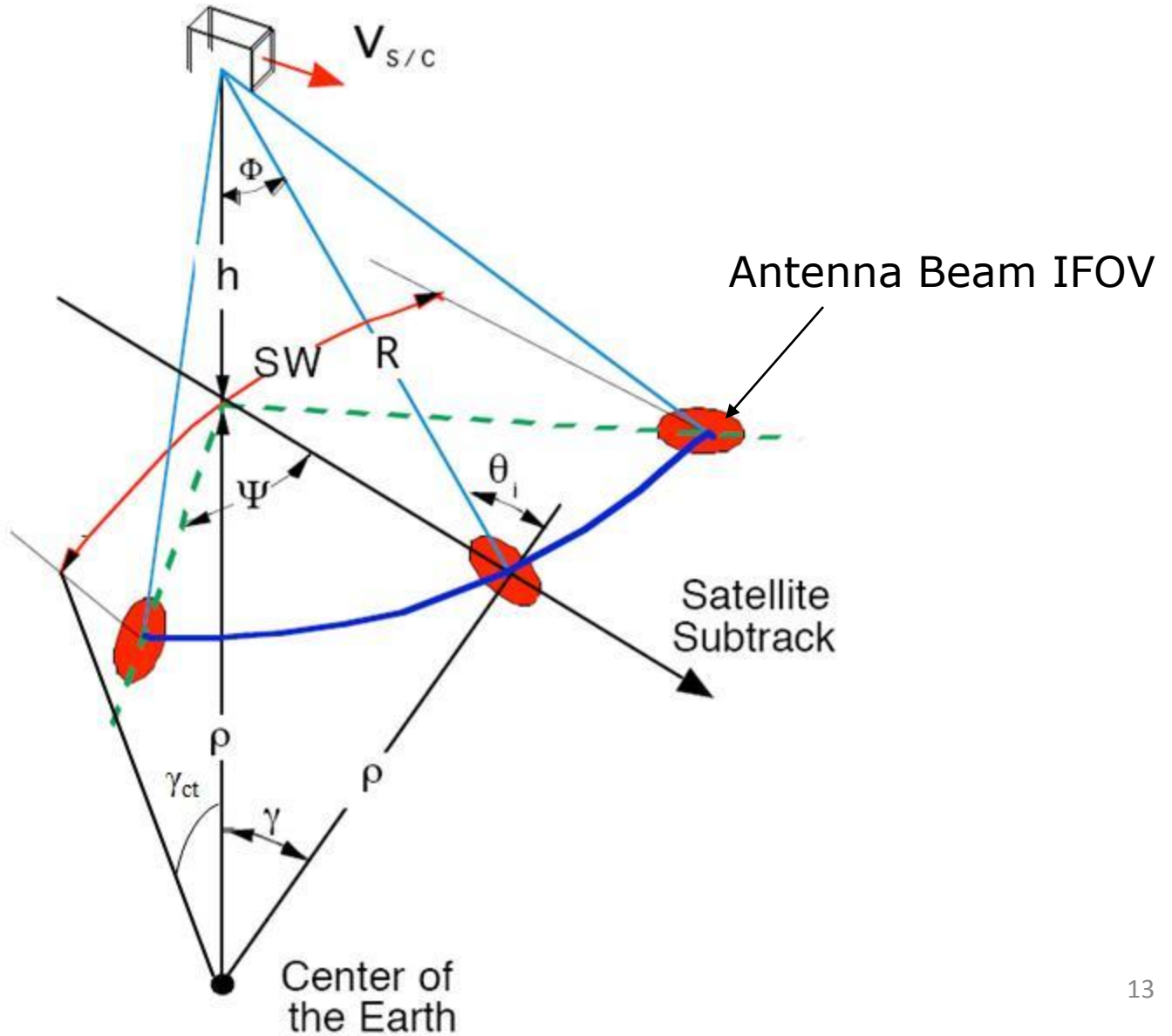
## Polar View



Note: Partial conical scan over  $\pm \Psi^\circ$  azimuth



# Conical Scanning Sensor Geometry cont.1



# MWR Swath Width

## Cross-Track Plane

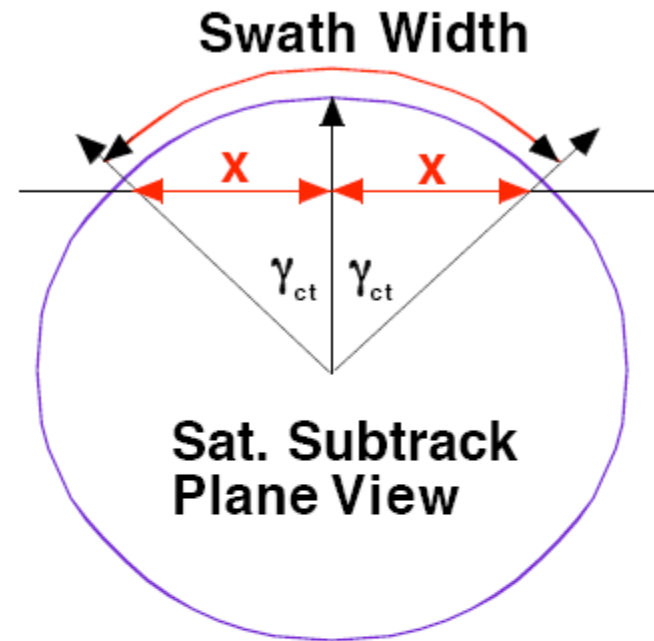
$$\sin(\gamma_{ct}) = \sin(\gamma) * \sin(\Psi)$$

$$\gamma_{ct} = \sin^{-1} \{ \sin(\gamma) * \sin(\Psi) \}$$

where  $\gamma$  is measured in incident plane

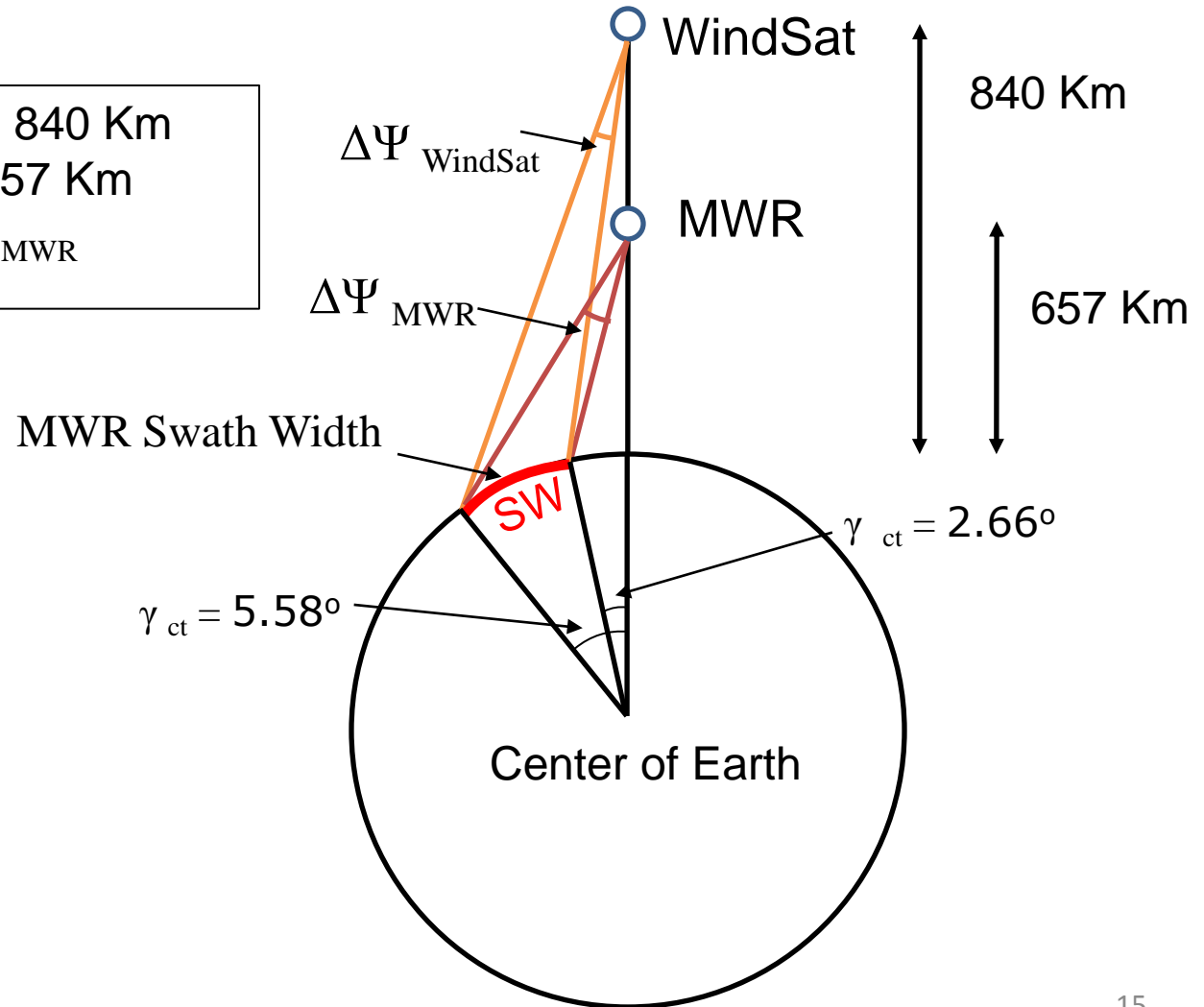
$$\text{Swath Width} = 2\rho\gamma_{ct} \quad \text{Note: } \gamma_{ct} \text{ is in units of radians}$$

Note: Swath width is measured in the cross-track plane



# Azimuthal Translation of MWR to Equivalent WindSat

- Altitude<sub>WindSat</sub> = 840 Km
- Altitude<sub>MWR</sub> = 657 Km
- $\Delta\Psi_{\text{WindSat}} < \Delta\Psi_{\text{MWR}}$

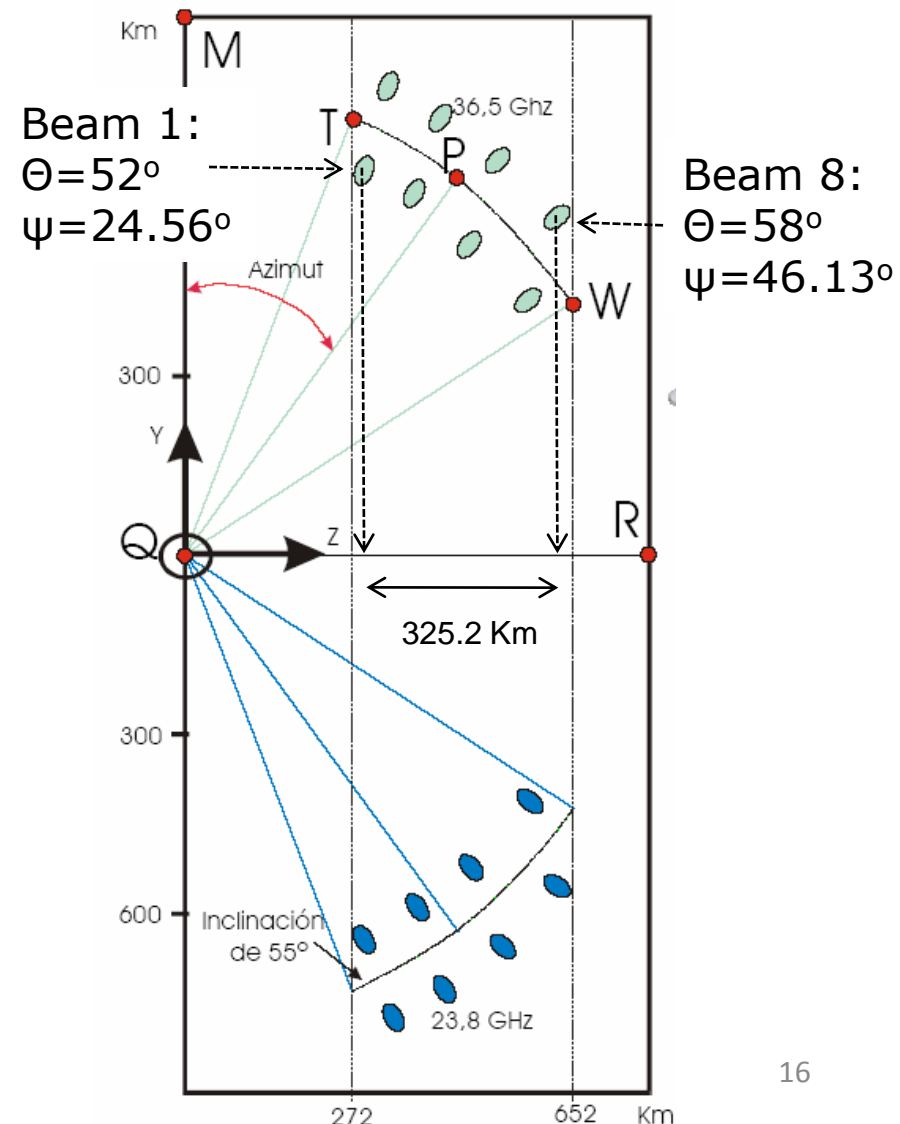


Satellite sub-track plane view

# Azimuthal Translation of MWR to Equivalent WindSat cont.

- MWR swath = 272 Km to 652 Km (to right of subtrack)
  - corres  $\gamma_{ct} = 2.66^\circ$  to  $5.58^\circ$
- Cross-track central angles ( $\gamma_{ct}$ ) are the same for MWR and WindSat; however central angles, ( $\gamma$ ) in the incident plane are different
  - MWR  $\gamma_{58} = 7.75^\circ$ ,  $\gamma_{52} = 6.40^\circ$
  - WindSat  $\gamma = 8.04^\circ$
- Using the equation,
 
$$\sin(\gamma_{ct}) = \sin(\gamma) \times \sin(\psi)$$
 solve for corresponding WindSat azimuth angles

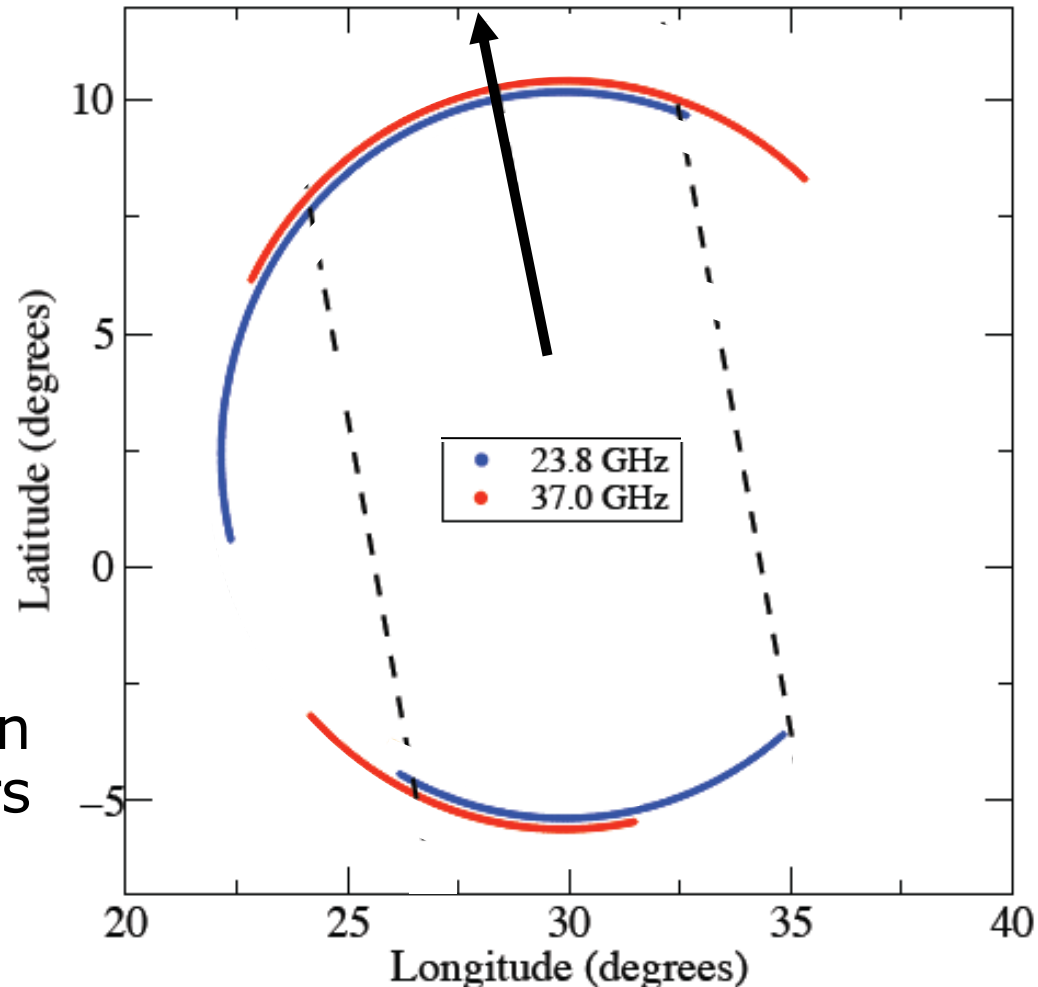
	Beam-1 (Az, deg)	Beam-8 (Az, deg)
MWR	24.56	46.13
WindSat	-19.37	-44.07





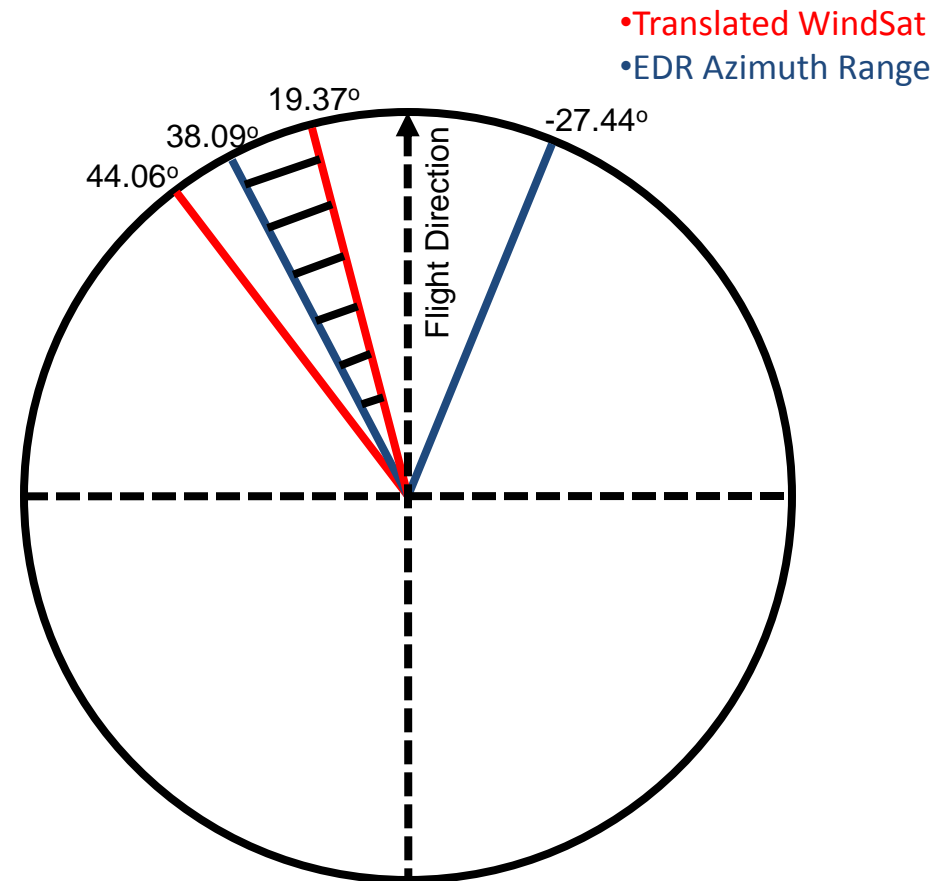
# WindSat Azimuth Constraints

- 37 GHz azimuth range
  - Fwd:  $-50^\circ$  to  $53^\circ$
  - Aft:  $125^\circ$  to  $183^\circ$
- 23.8 GHz azimuth range
  - Fwd:  $-28^\circ$  to  $94^\circ$
  - Aft:  $142^\circ$  to  $211^\circ$
- For geophysical retrievals, forward and aft beams of MWR must be collocated
- Mirror the MWR swath on the left side, which offers sufficient common forward swath



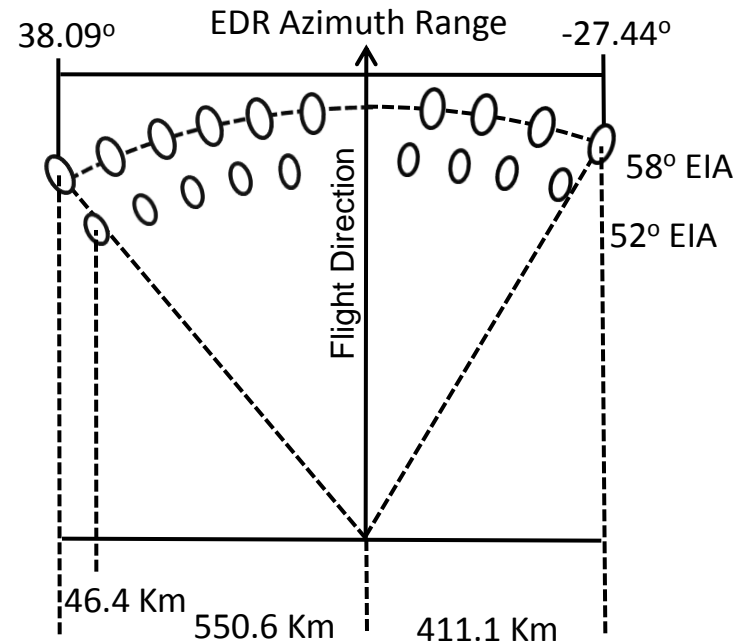
# WindSat Envir Data Record (EDR) Azimuth Constraints

- The EDR imposes a limit on the usable azimuth angles
  - EDR azimuth range  
-27.44° to 38.09°
- Left sided MWR mirrored swath will lose  $\sim 6^\circ$  in azimuth; therefore swath is shifted to start from 38.09°
- Additional MWR beams generated using the entire azimuth range of EDR



# WindSat EDR Azimuth Constraints

- A total of 19 MWR beams have been simulated
  - 11 on the left & 8 on the right side of flight direction
- Left most MWR beam corresponds to swath width of 550.6 Km & right most corresponds to 411.1 Km
- The beam center to center swath spacing corresponds exactly to MWR spacing = 46.4 Km (325.2/ 7)
- Accurate spatial & sampling resolution of MWR
- Accurate orientation by change in azimuth



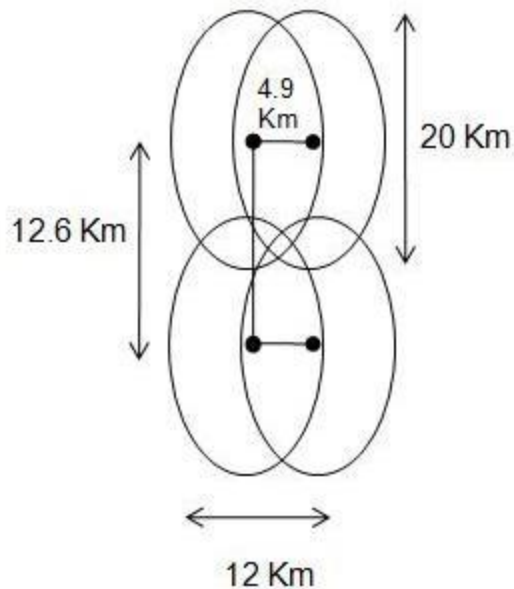
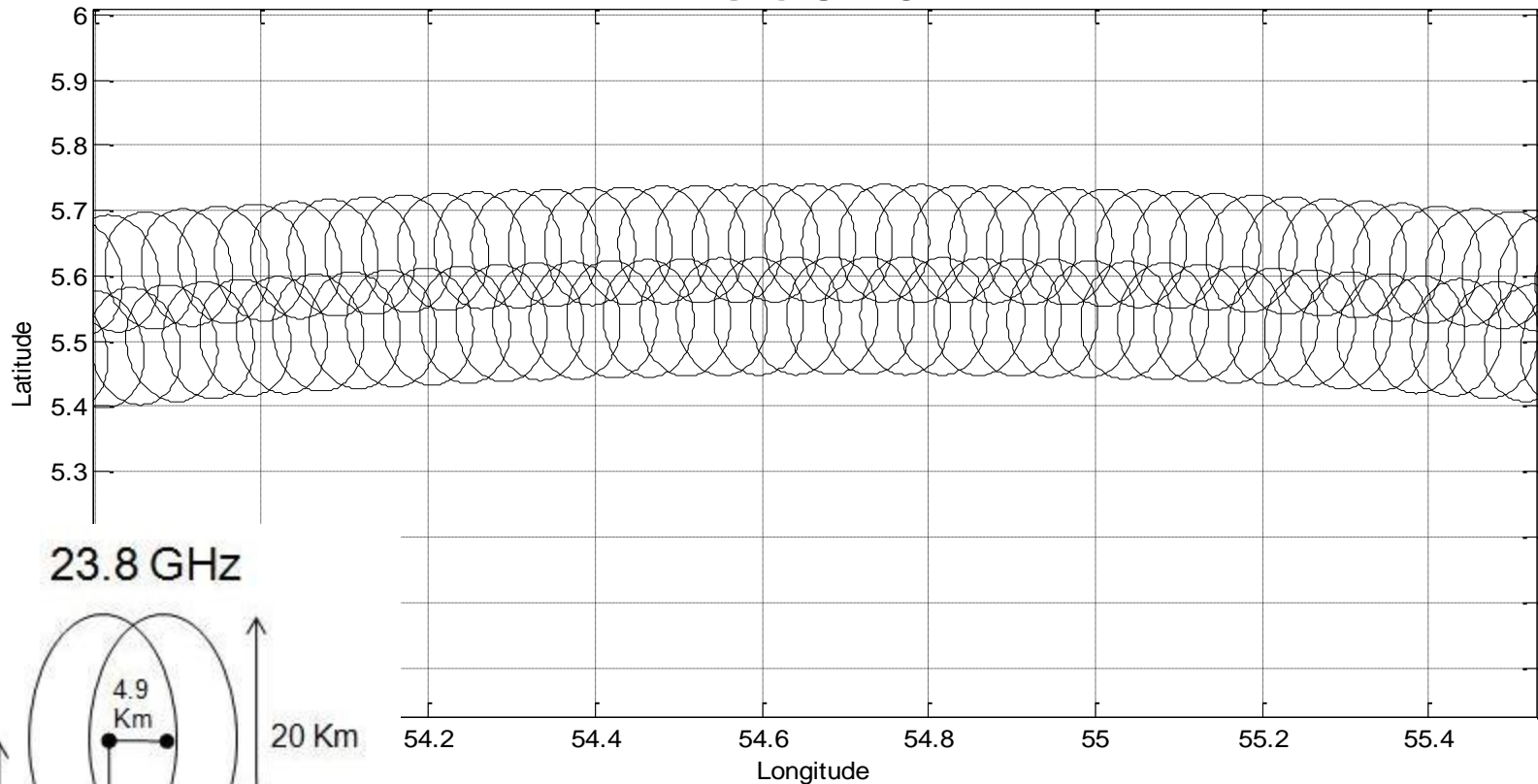
- Beam Azimuth Angle:

$$\gamma_{ct} = \text{Swath width} / \rho$$

$$\Psi_{\text{beam}} = \sin^{-1} (\sin(\gamma_{ct}) / \sin(\gamma_{\text{WindSat}}))$$

- The 8 beams on either side of flight direction are symmetrical by azimuth

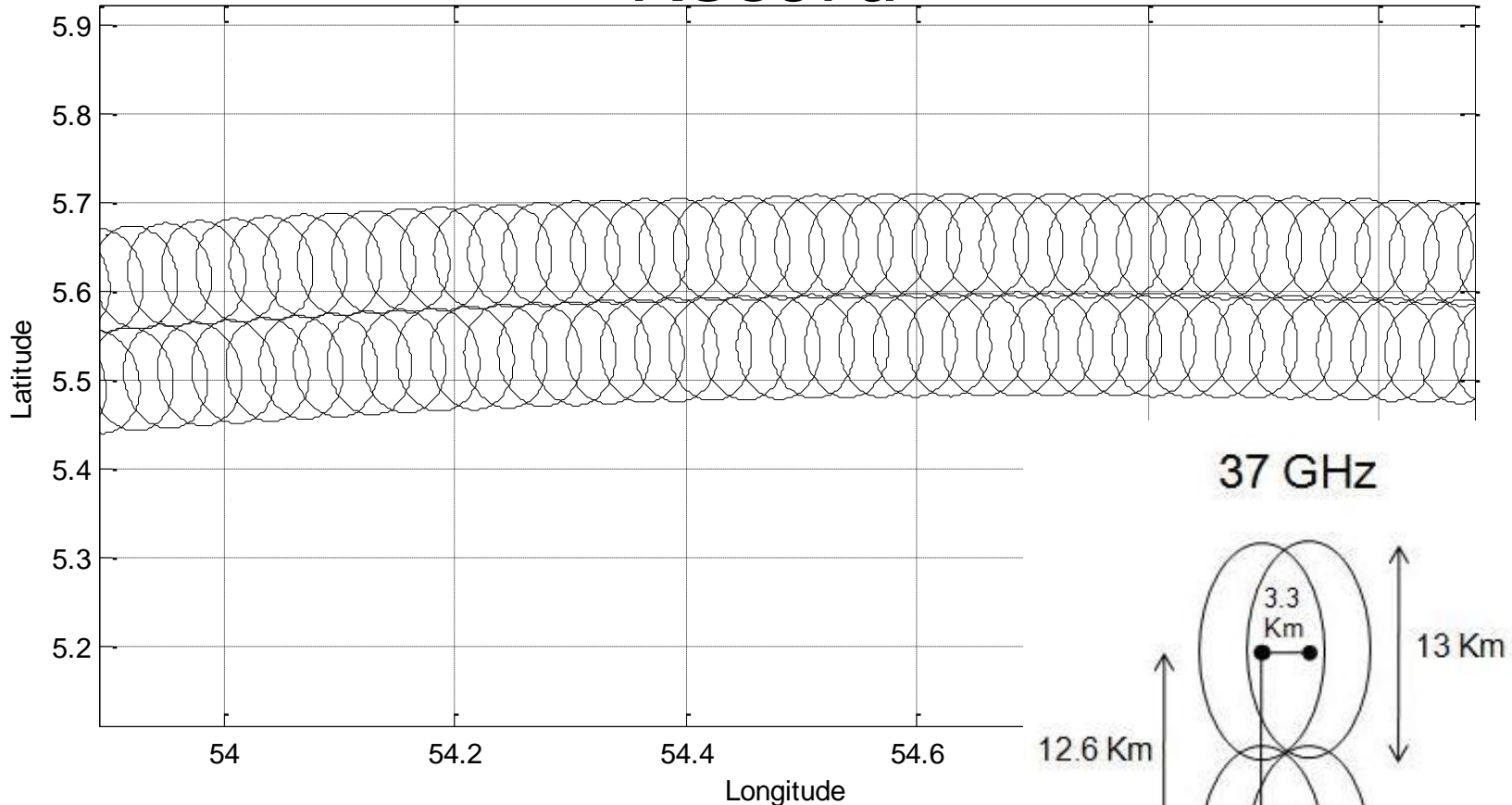
# 23.8 GHz WindSat Intermediary Data Record



- High resolution spatial sampling along a conical scan
- Resolution  $_{23 \text{ GHz}} - 12 \times 20 \text{ Km}$
- $\Delta\psi_{23.8} = 0.313^\circ/\text{pixel}$

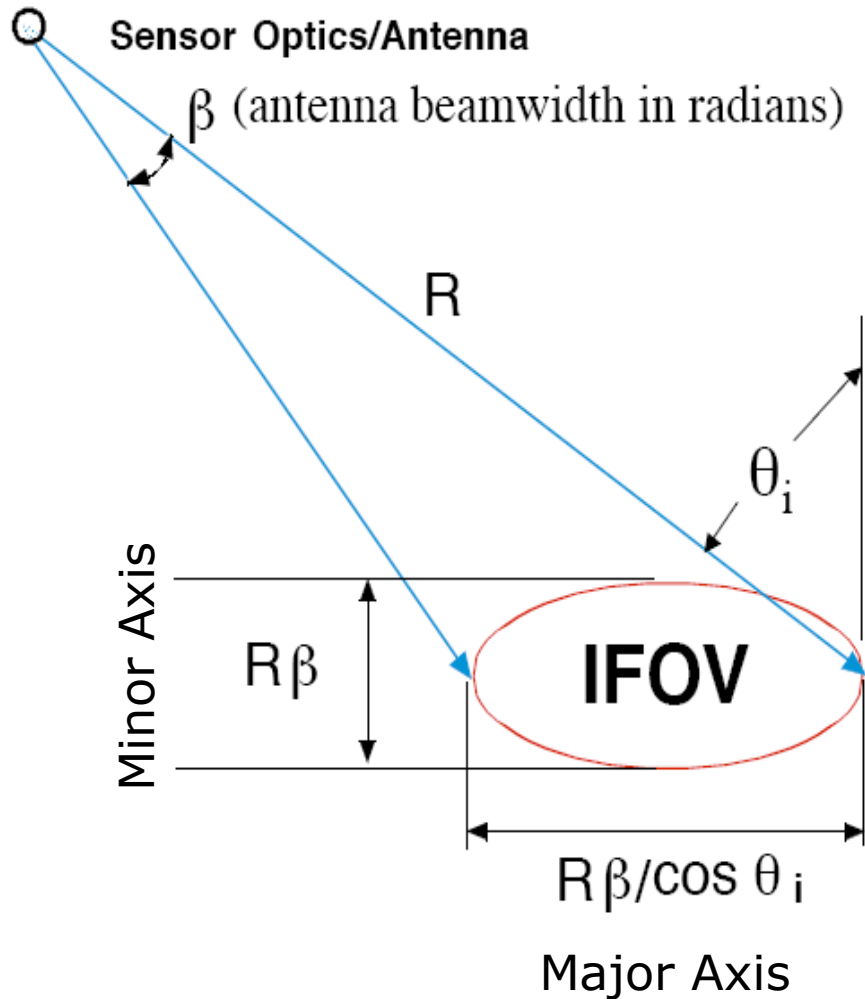


# 37 GHz WindSat Intermediary Data Record



- High resolution spatial sampling along a conical scan
- Resolution  $_{37 \text{ GHz}} - 8 \times 13 \text{ Km}$
- $\Delta\psi_{23.8} = 0.21^\circ/\text{pixel}$

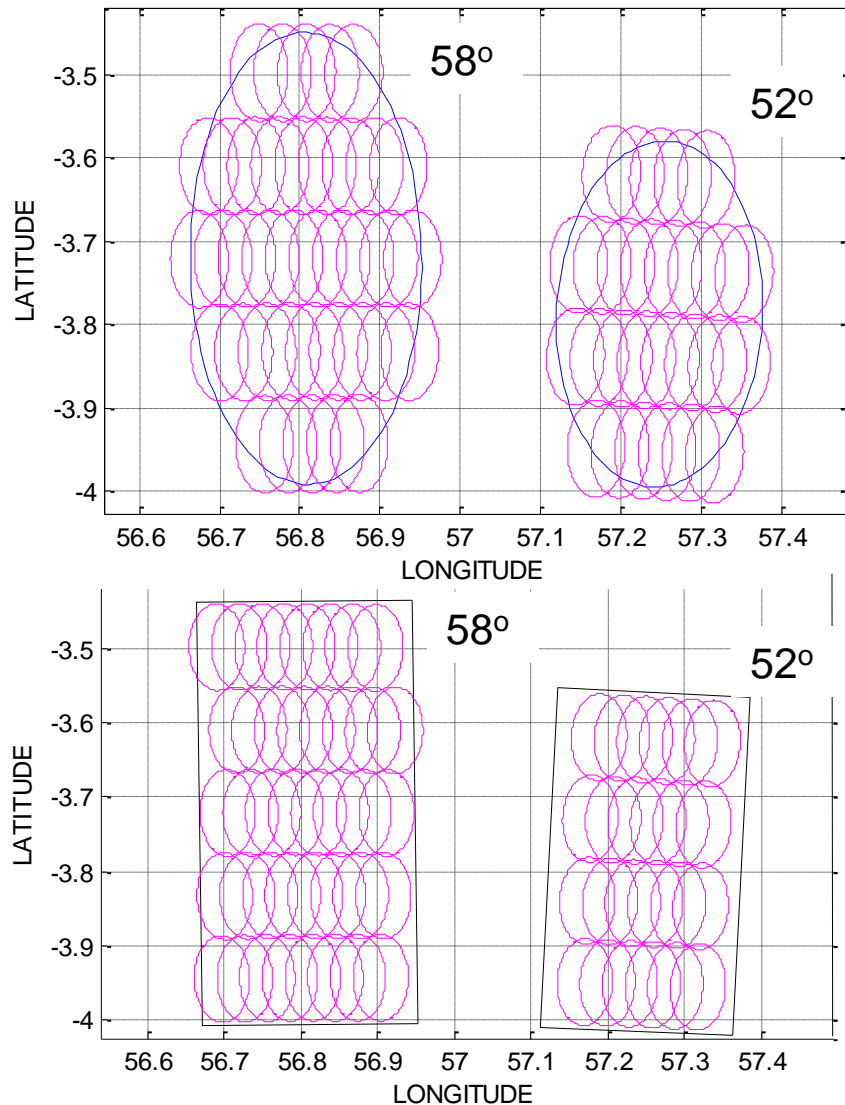
# MWR IFOV Geometry



- MWR footprint dimensions
- $\Theta = 52^\circ$  &  $58^\circ$
- 3 dB beam width,  $\beta = 1.64^\circ$
- Slant range:
  - $R_{58} = 1118.6$  Km
  - $R_{52} = 995.8$  Km

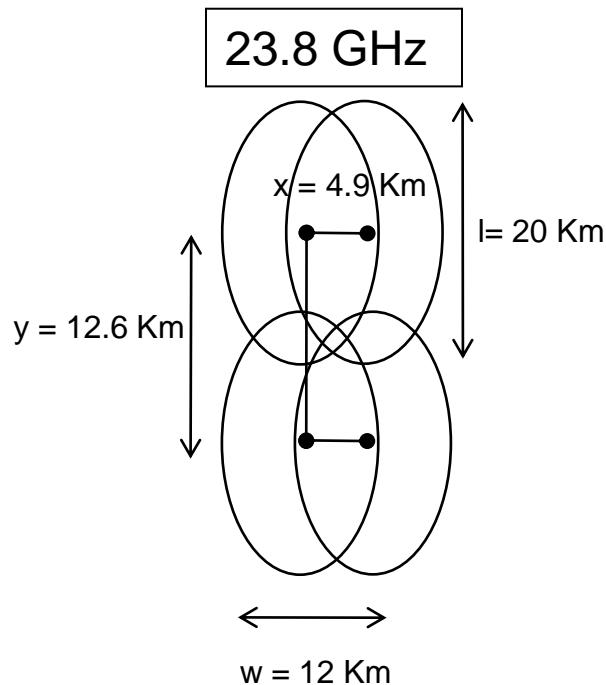
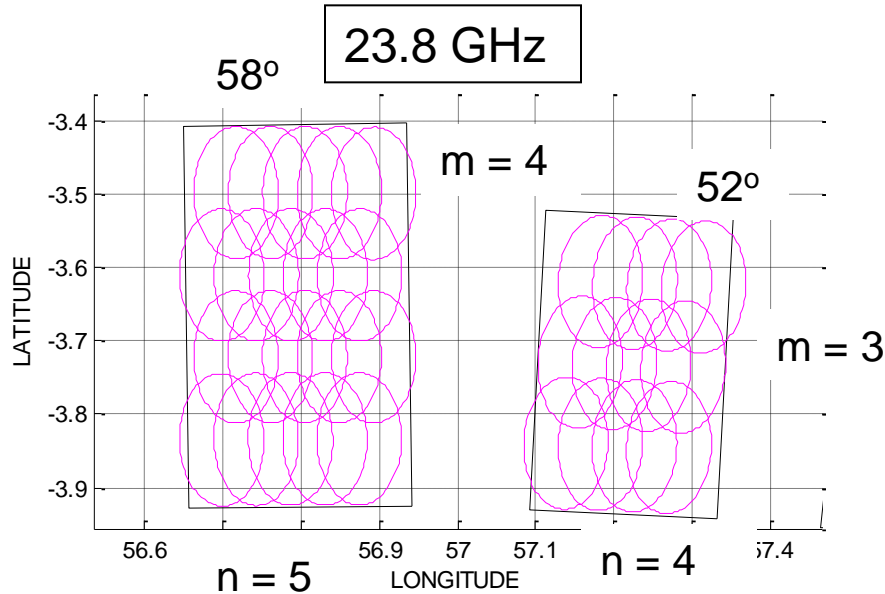
Incidence Angle	Minor Axis (Km)	Major Axis (Km)
$52^\circ$	28.5	46.3
$58^\circ$	32	60.4

# 37 GHz IDR Beam-Fill in MWR IFOV



- Number of along-scan IDR pixels falling into an elliptical footprint varies along ellipse major axis
- Complexity is reduced using a rectangular footprint
- Rectangular footprint has equal number of along-scan IDR pixels for all scans

# 23.8 GHz IDR Beam-Fill in MWR IFOV cont.



- The IDR pixels falling into a rectangular footprint, along-scan & along-track, are calculated with the following equations

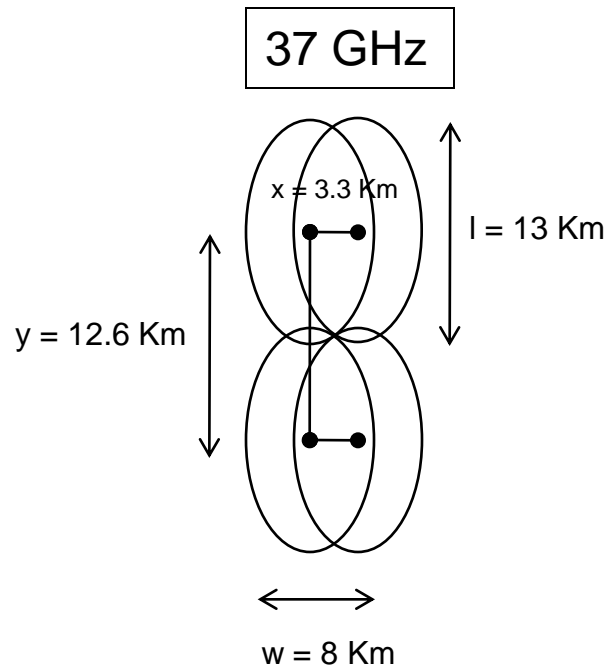
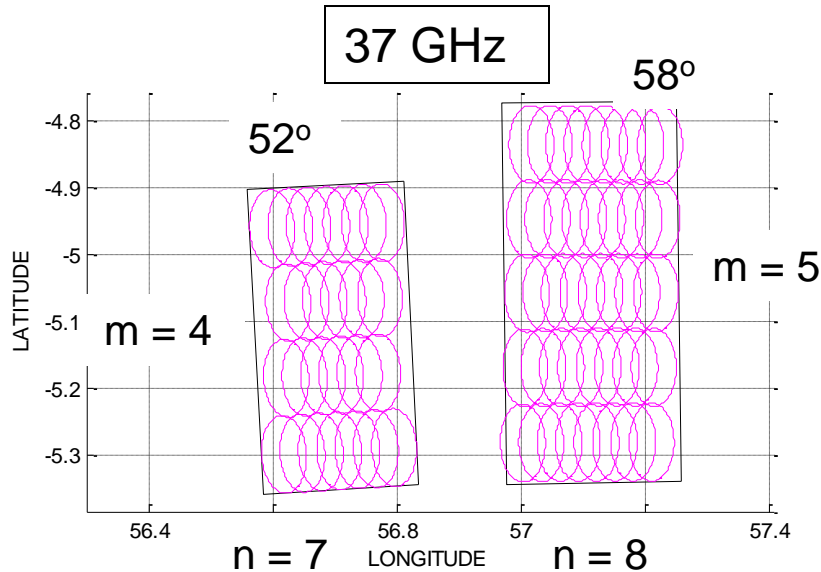
$$n = ((MinorAxis - w) / x) + 1$$

$$m = ((MajorAxis - l) / y) + 1$$

- 'n' is the integer # of IDR pixels along-scan while 'm' is integer the # of IDR scans

Incidence Angle	Minor Axis (Km)	Major Axis (Km)	n	m
52°	28.5	46.3	4	3
58°	32	60.4	5	4

# 37 GHz IDR Beam-Fill in MWR IFOV cont.



- The IDR pixels falling into a rectangular footprint, along-scan & along-track, are calculated with the following equations

$$n = ((\text{MinorAxis} - w) / x) + 1$$

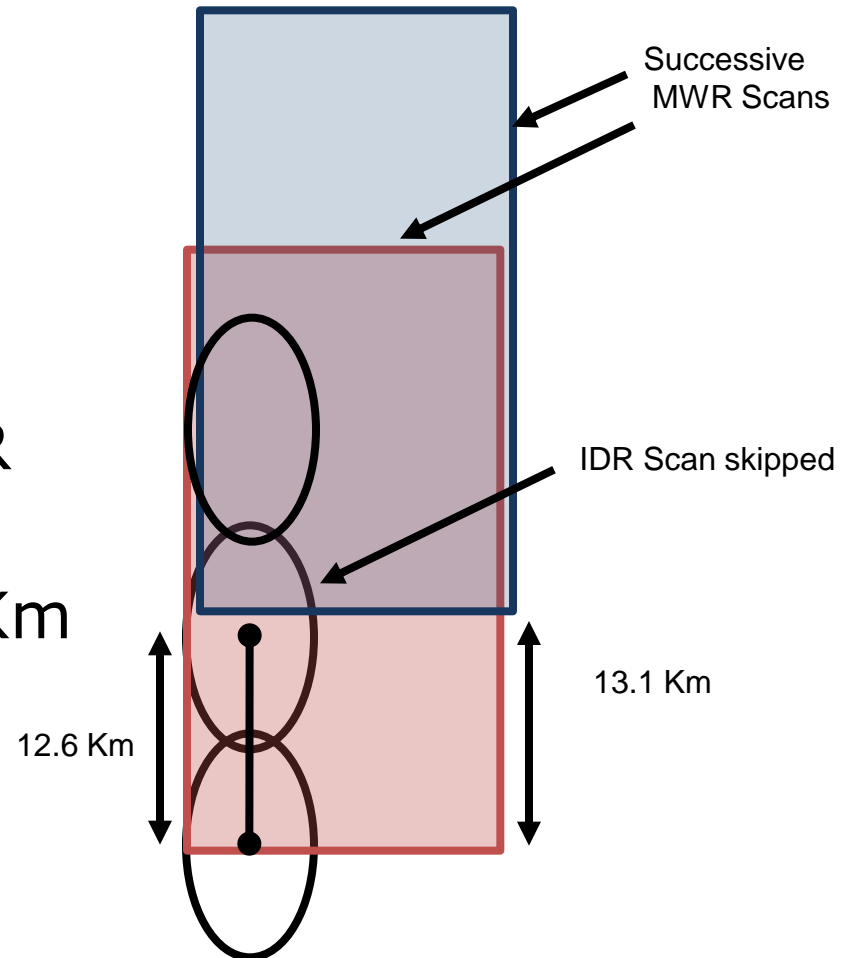
$$m = ((\text{MajorAxis} - l) / y) + 1$$

- 'n' is the integer # of IDR pixels along-scan while 'm' is the integer # of IDR scans

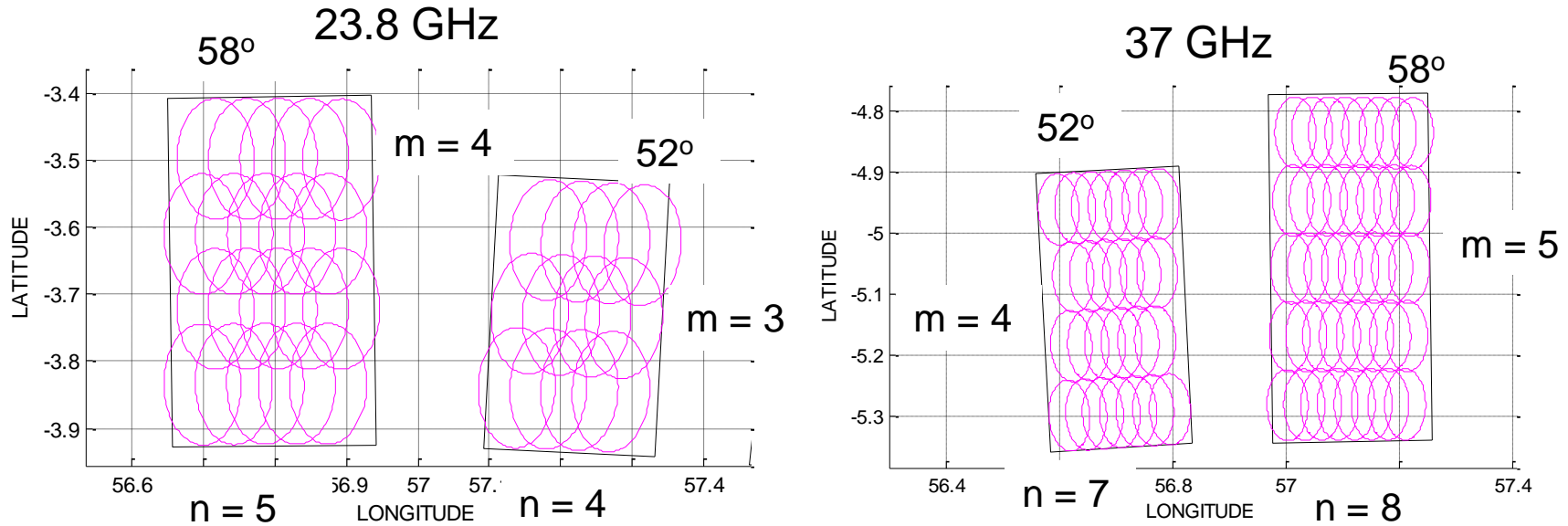
Incidence Angle	Minor Axis (Km)	Major Axis (Km)	n	m
52°	28.5	46.3	7	4
58°	32	60.4	8	5

# IDR Scan Mapping into MWR Pixels

- MWR Inter-scan distance = 13.1 Km
- IDR Inter-scan distance = 12.6 Km
- Difference = 0.5 Km; therefore periodically an IDR scan will be skipped
- This period is  $12.6 \text{ Km} / 0.5 \text{ Km} = 25.2$  scans



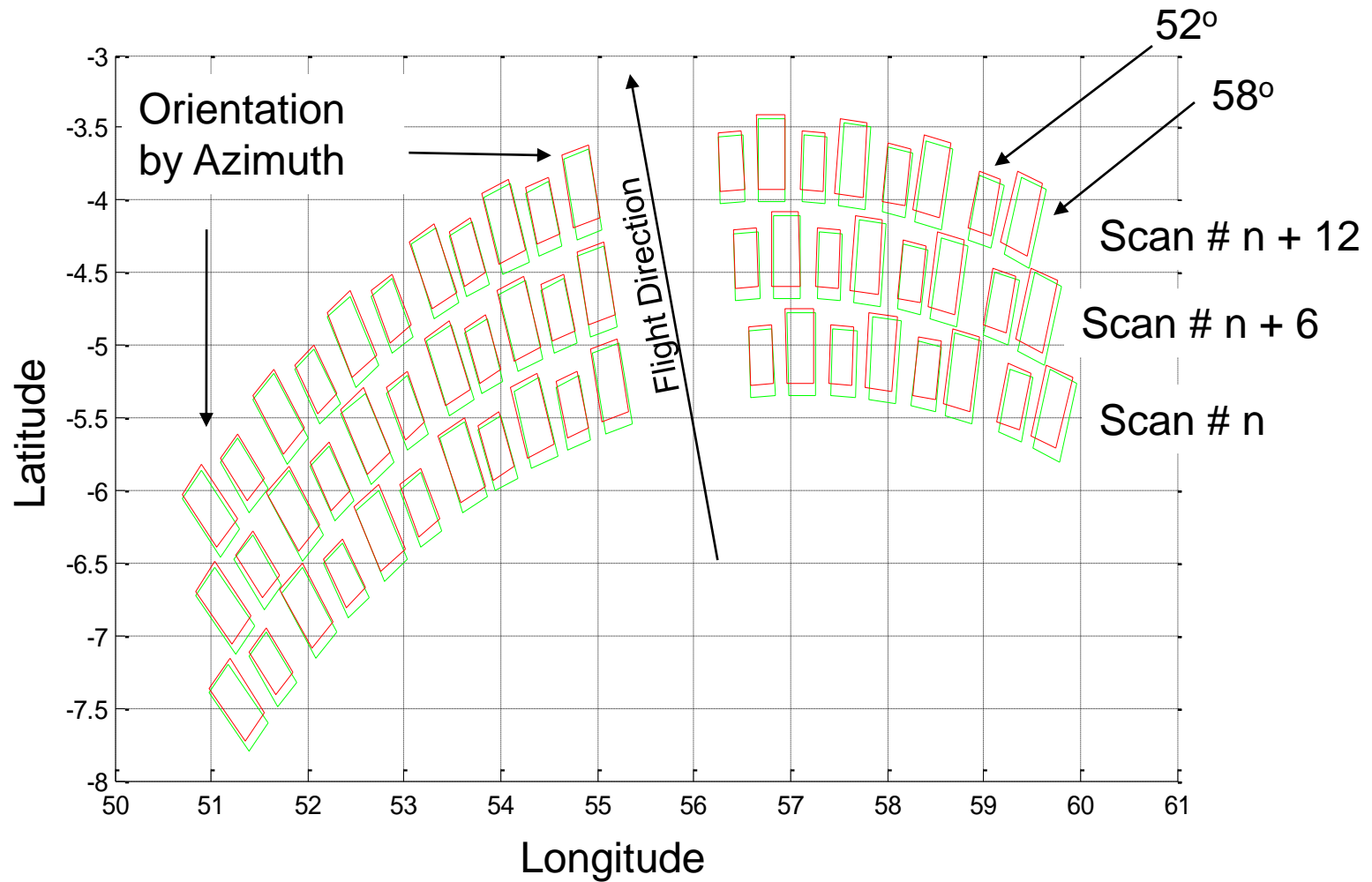
# MWR IFOV Summary



Frequency	Incidence Angle	Width (Km)	Length (Km)	IDR Pixels n (Across Track)	IDR Scans m (Along Track)
23.8 GHz	58°	31.6	57.8	5	4
	52°	26.7	45.2	4	3
37 GHz	58°	31.1	63.4	8	5
	52°	27.8	50.8	7	4

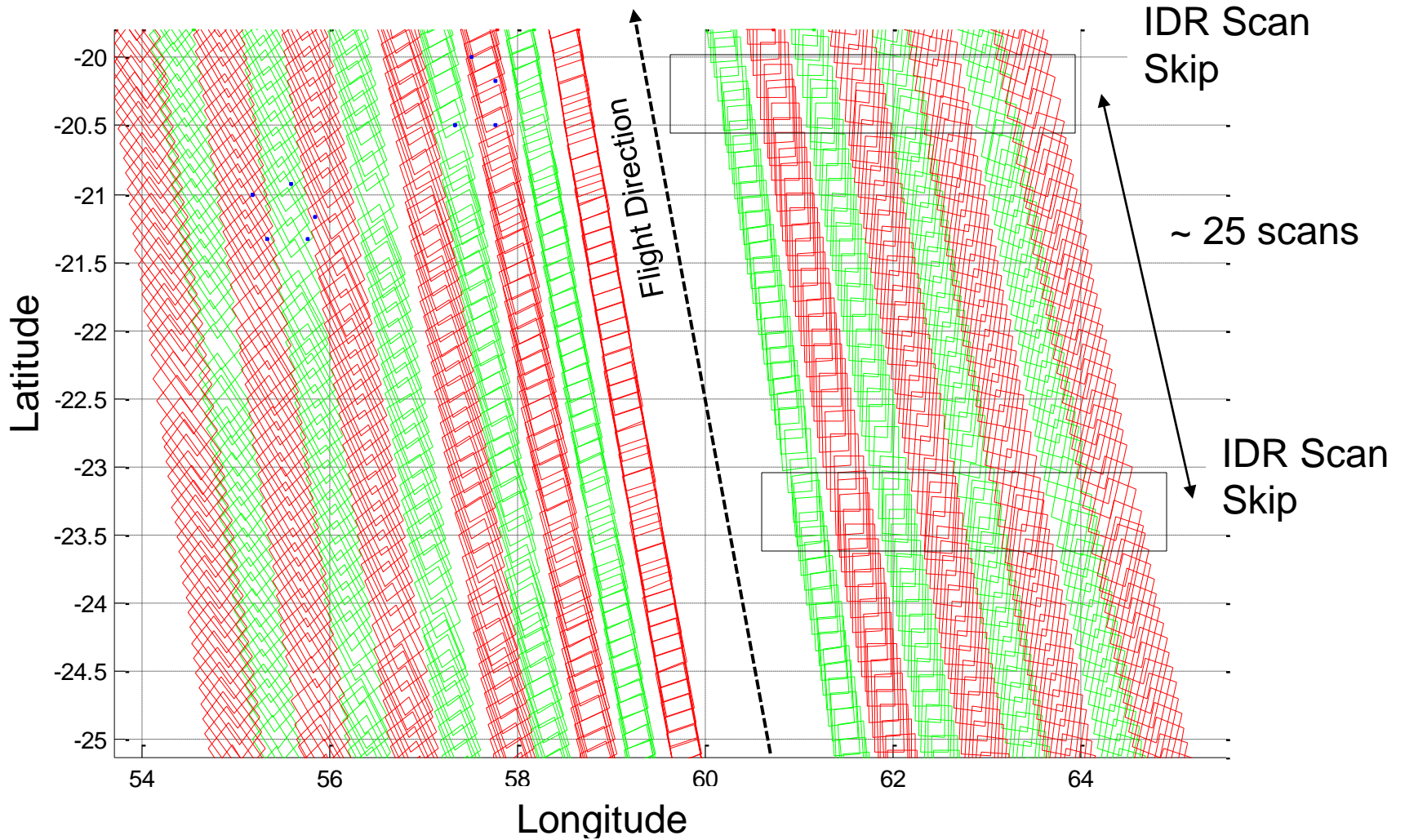


# MWR Pixel Collocations

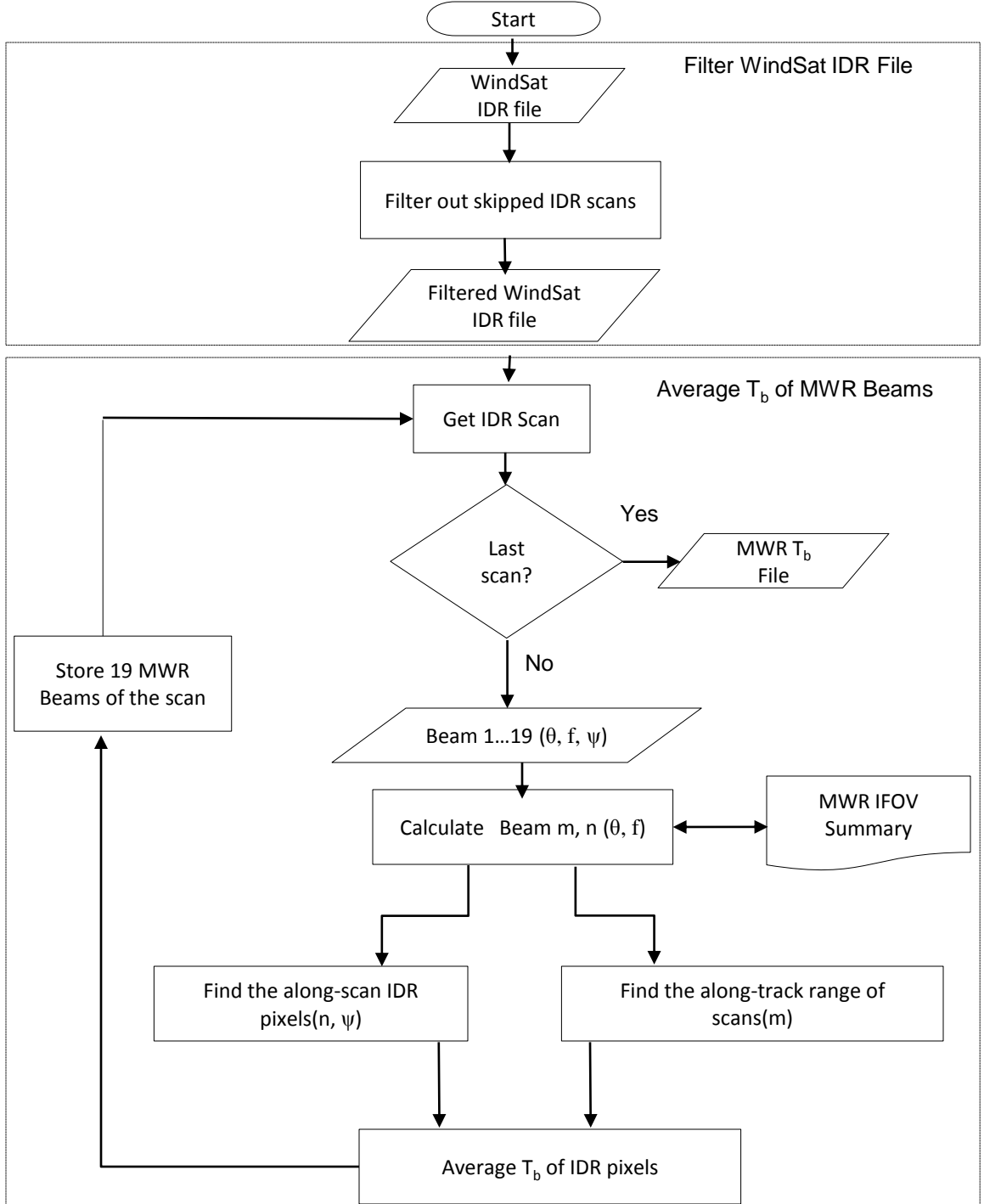


Collocated 23.8 (Green) & 36.5 (Red) GHz Beams

# MWR 37 GHz Pixels

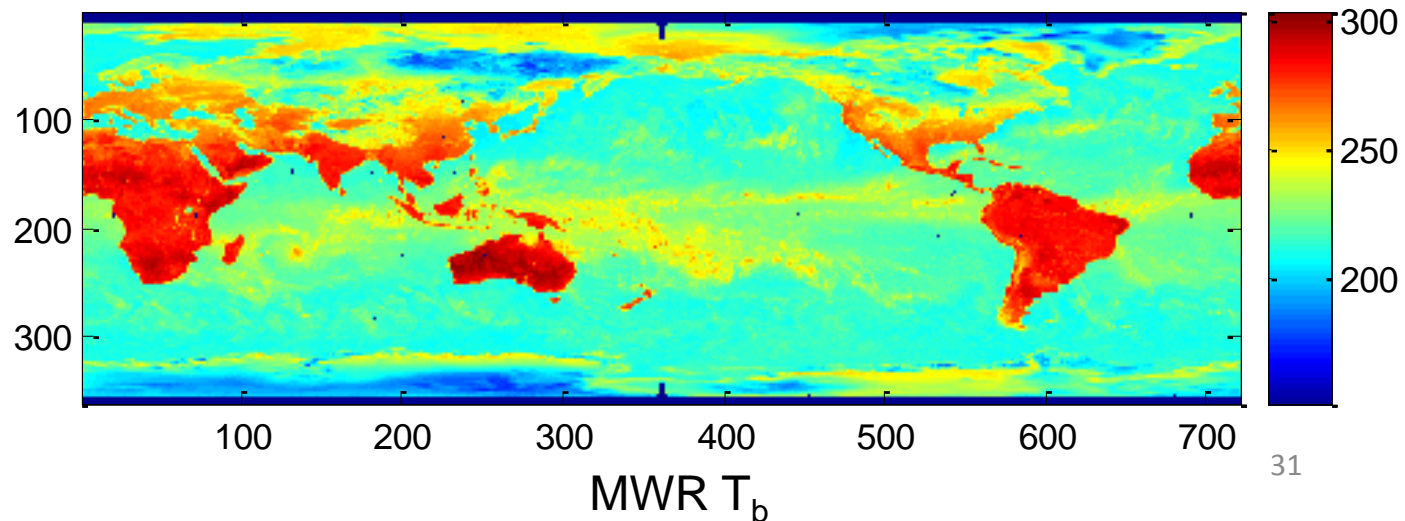
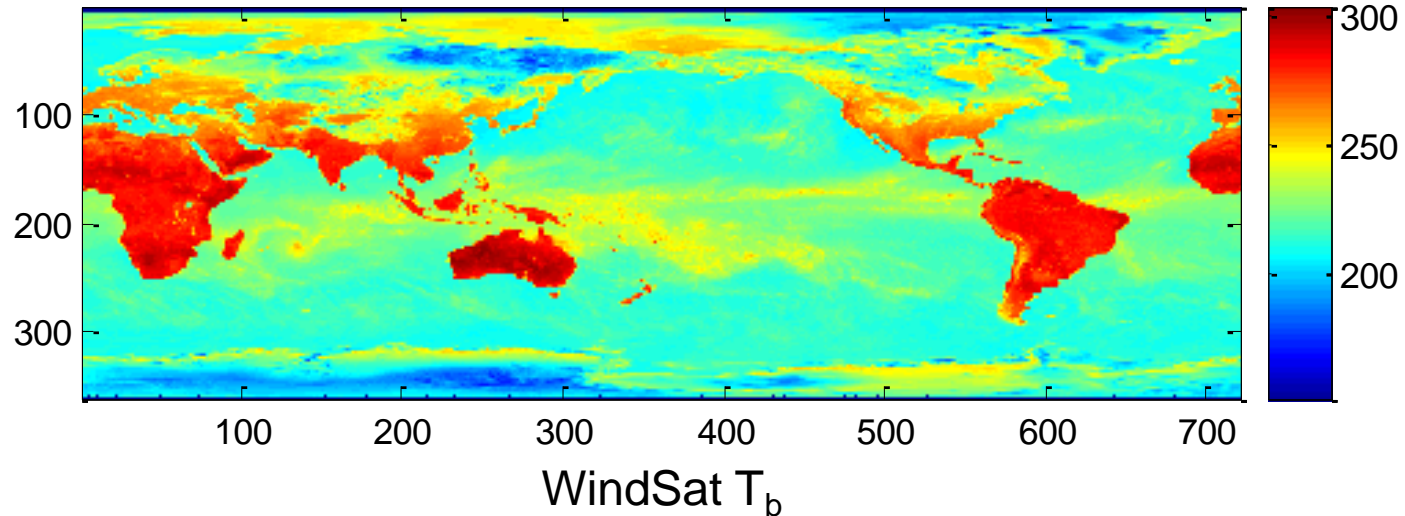


MWR 36.5 GHz Swath at 58° (Red) & 52° (Green)



# Comparison of WindSat & MWR $T_b$ at 37 GHz (V-pol) @ 53 deg

- $0.5^\circ$  resolution
- $T_b$  average of 68 orbits in Feb 2007
- Shows radiometric accuracy of the  $T_b$  simulation
- Mean  $\Delta T_b = 0$  K
- $\sigma \Delta T_b = \sim 2$  K



# $T_b$ Normalization

- WindSat  $T_b$  normalizations are required for incidence angle & frequency adjustment
  - WindSat operates at 23.8 - & 37-GHz @  $53^\circ$
  - MWR operates at 23.8 - & 36.5-GHz @  $52^\circ$  &  $58^\circ$
- Radiative Transfer Model (RTM) was used to transform WindSat  $T_b$  measurements to equivalent MWR frequencies and incidence angles

# WindSat Normalization Procedure

- Run RTM
  - Calculate theoretical MWR  $T_b$  for environmental parameters ( $1^\circ$  box)
    - $Tb_{(MWR\text{-predicted})}(f_{MWR}, \Theta_{MWR}, WS, SST, WV, CLW)$ 
      - Frequency = 23.8- & 36.5 GHz
      - Incidence angle =  $52^\circ$  &  $58^\circ$
  - Calculate theoretical WindSat  $T_b$  for environmental parameters ( $1^\circ$  box)
    - $Tb_{(WS\text{-predicted})}(f_{WS}, \Theta_{WS}, WS, SST, WV, CLW)$ 
      - Frequency = 23.8- & 37 GHz
      - Incidence angle =  $53^\circ$

# Expected Delta Tb (MWR to WindSat)

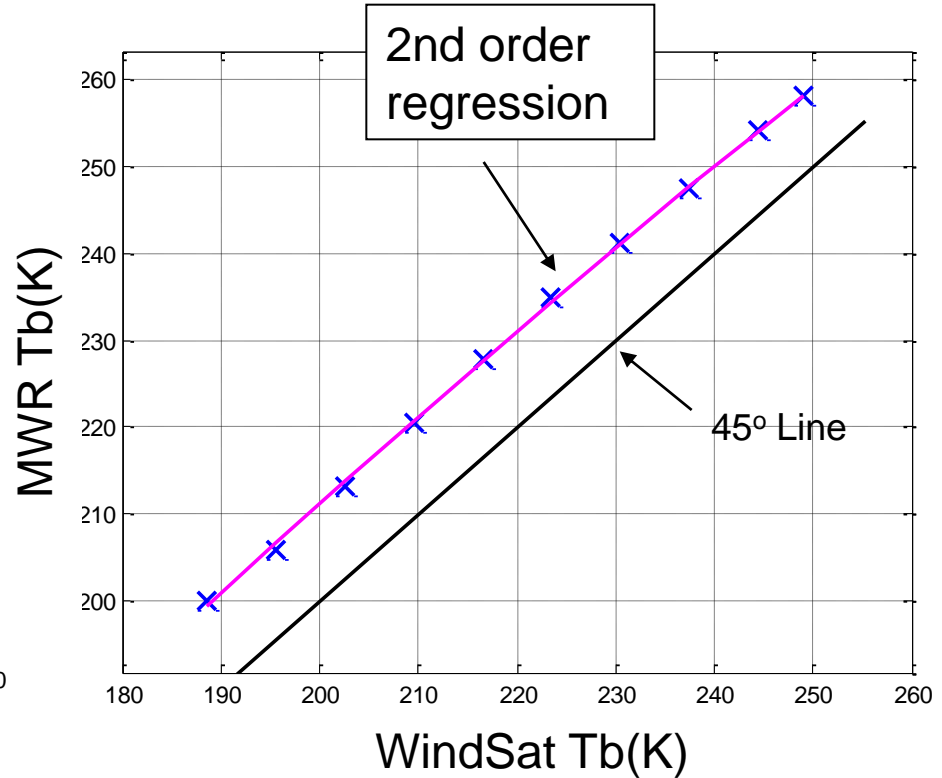
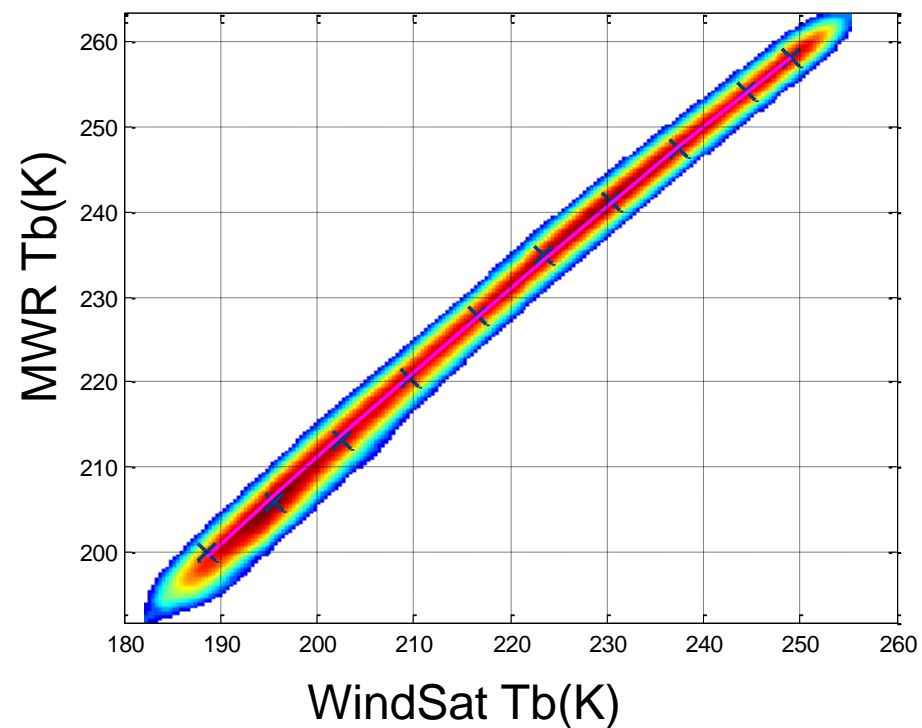
– Calculate the predicted (theoretical) Tb difference between MWR & WindSat

- $\text{delta} = \text{MWR}_{\text{predicted}} - \text{WS}_{\text{predicted}}$

$$T_{b \text{ MWR}} = \text{WindSat}_{(\text{measured})} + \text{delta}$$



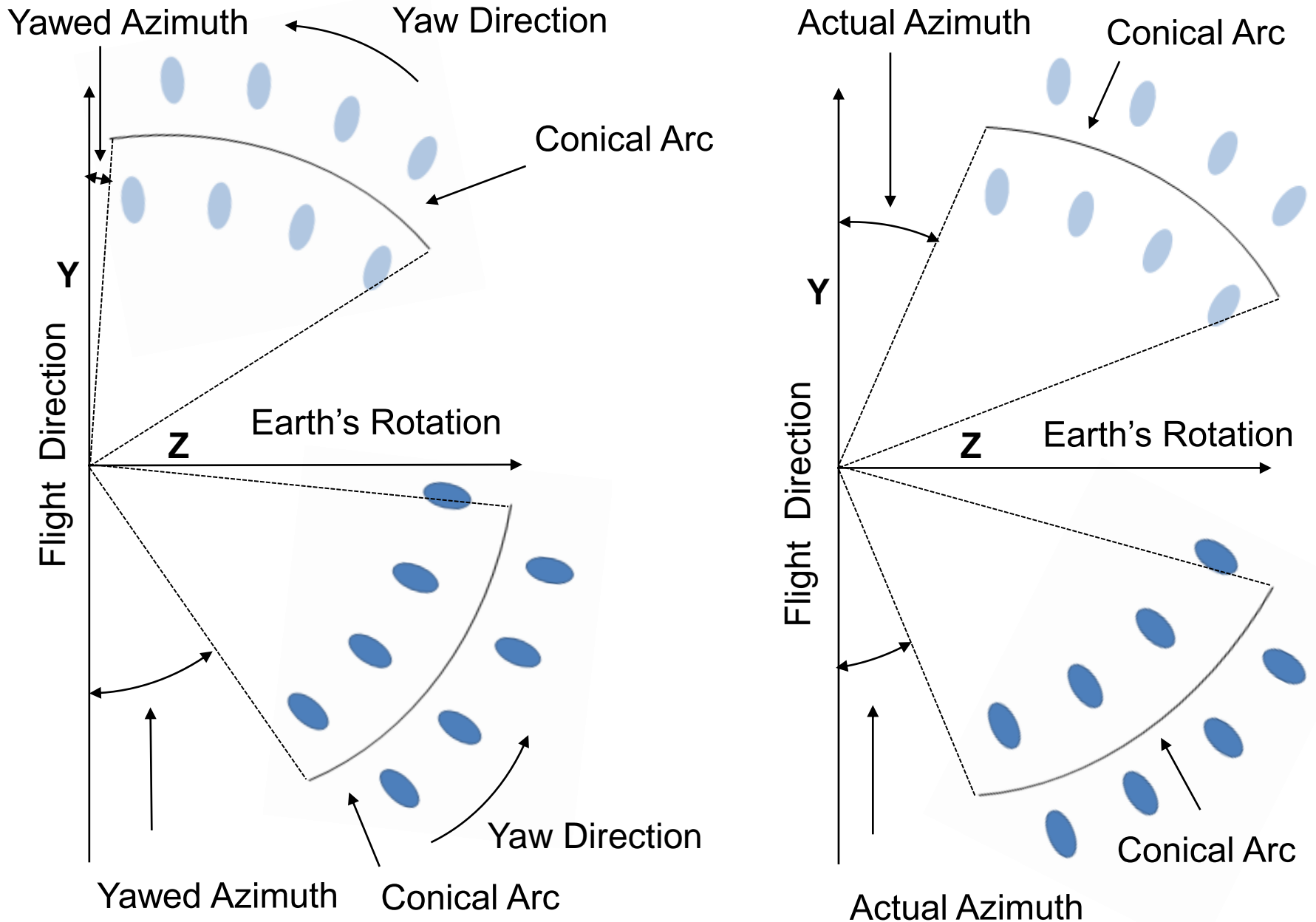
# $T_b$ Normalization of 23.8 V Channel ( $58^\circ$ )



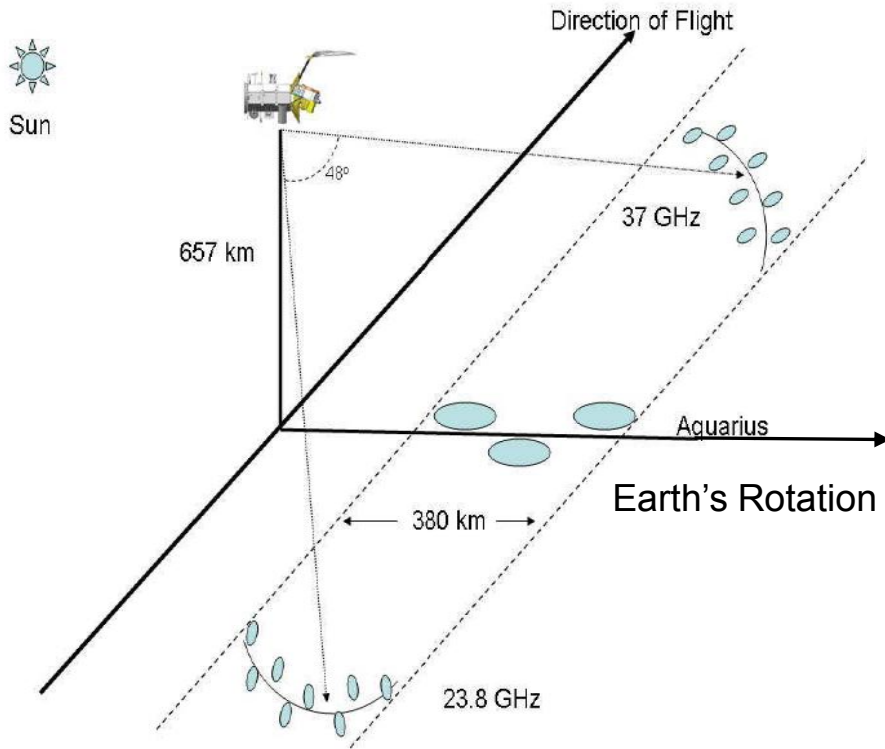
- Ran RTM for 1 week to calculate WindSat & MWR theoretical  $T_b$  s
- $T_b$  (theoretical) (  $f$ ,  $\Theta$ ,  $WS$ ,  $SST$ ,  $WV$ ,  $CLW$  ), envr. parameters from GDAS
- $T_b$  normalizations were done for all channels (23.8 V, 36.5 V & H) at  $52^\circ$  &  $58^\circ$  incidence angles
- The  $T_b$  Biases were found to be independent of the environmental variables

# Yaw Steering Results

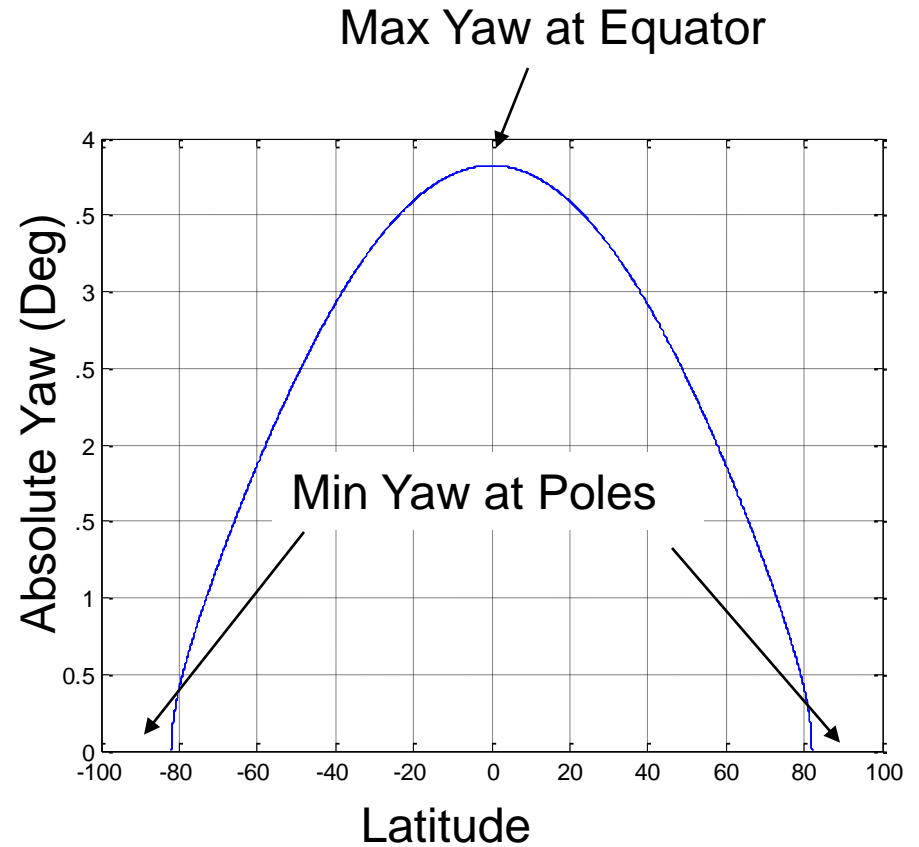
# Aquarius/SAC-D Yaw Steering



# Aquarius/SAC-D Yaw Steering



Collocated MWR & Aquarius Swath

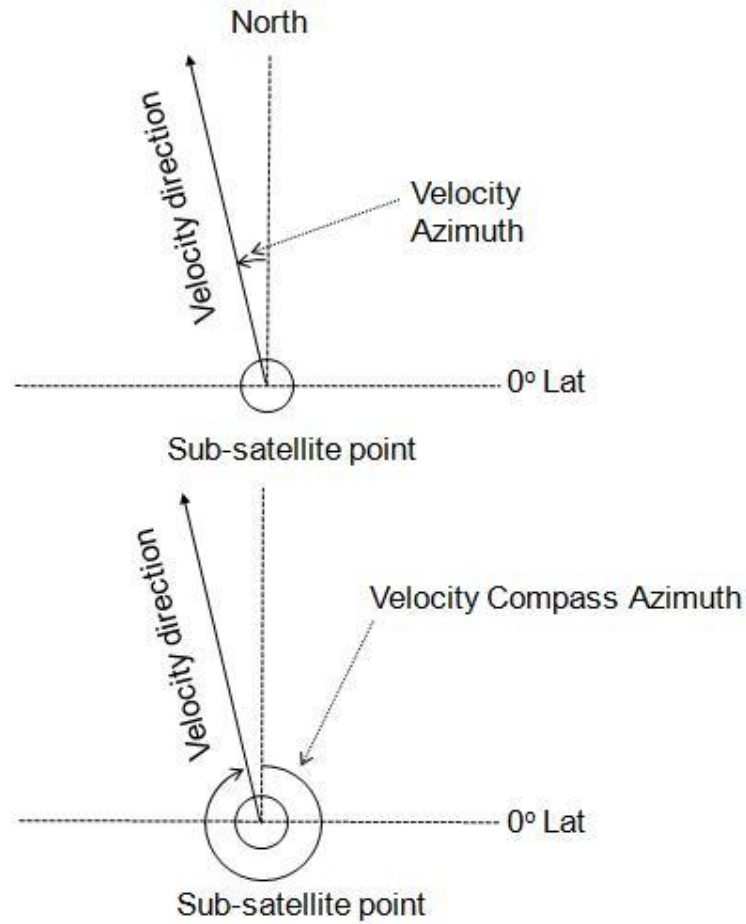


Absolute Yaw as a function of Latitude (Provided by CONAE)

# Evaluation Procedure

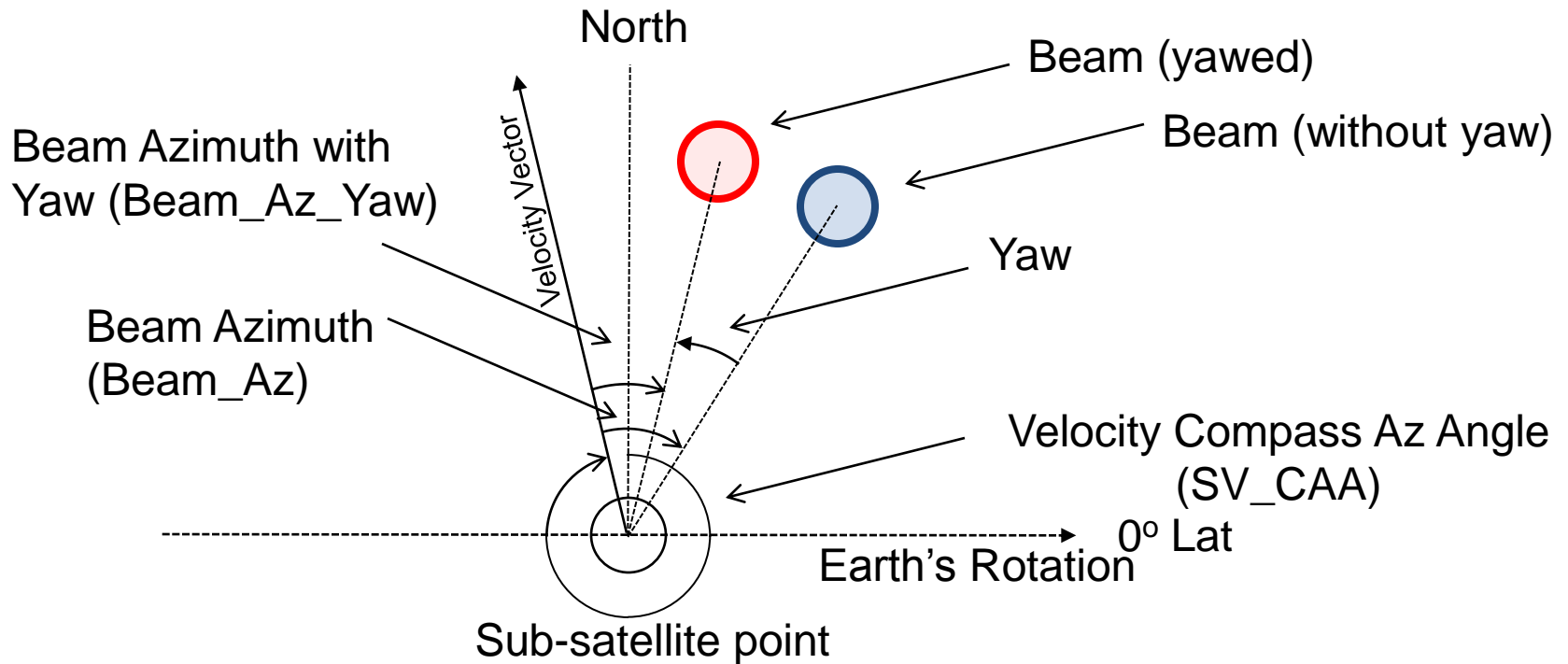
- Used STK to simulate SAC-D orbit (Inclination  $98^\circ$ , Eccentricity = 0, Altitude = 657 Km) & generated:
  - SSPs
  - Satellite Velocity Azimuth (relative to North)
  - @ 0.24 sec time step
- Generated corresponding pairs of forward/aft beam points sequentially for 8 pairs @ 0.24 sec step, using:
  - SubSat Point (SSP) (lat, lng)
  - Earth Central Angle ( $\gamma$ ) b/w SSP & beam boresight
  - Beam Compass Azimuth (+ Yaw @ SSP\_lat)

# Evaluation Procedure cont.



Satellite Velocity Azimuth

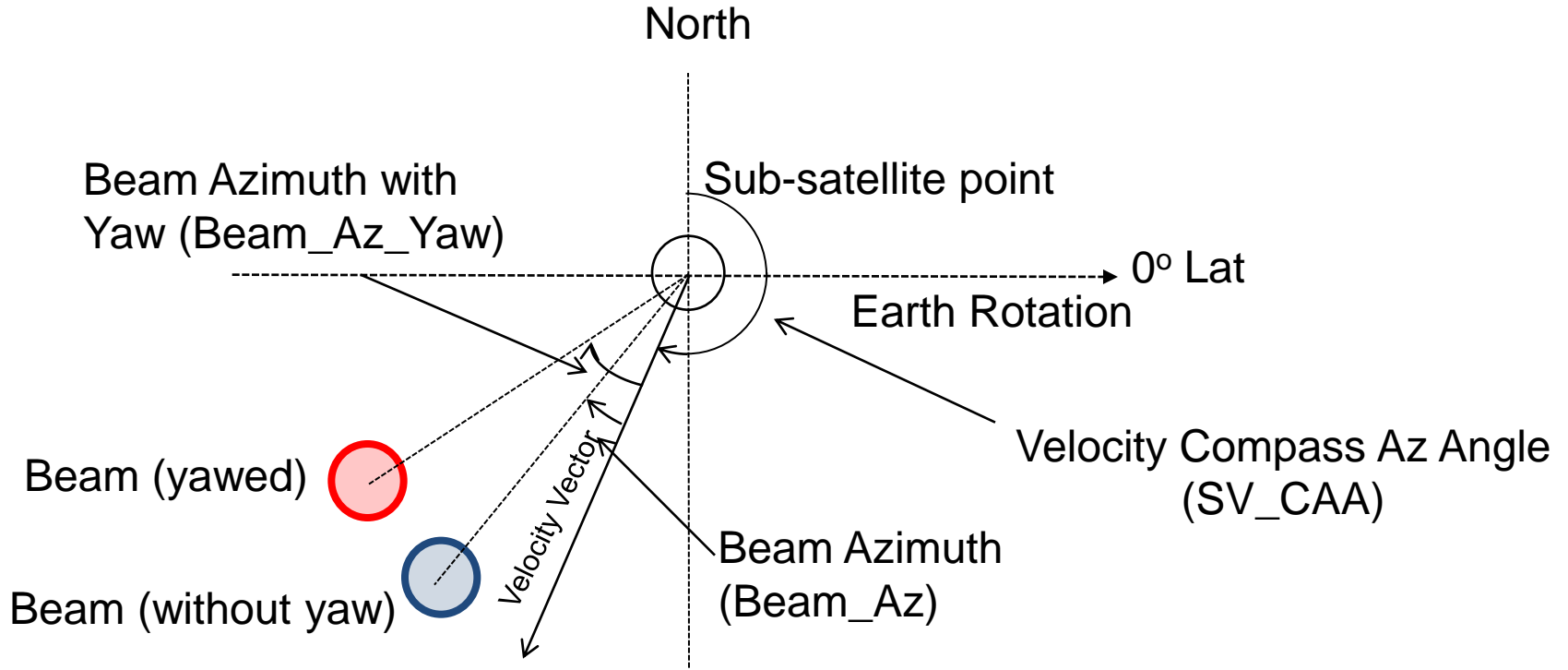
# Beam Compass Azimuth Angle for Ascending Flight



$$\text{Beam\_CAA\_Yaw} = \text{modulo} ((\text{SV\_CAA} + \text{Beam\_Az} + \text{Yaw}), 360)$$

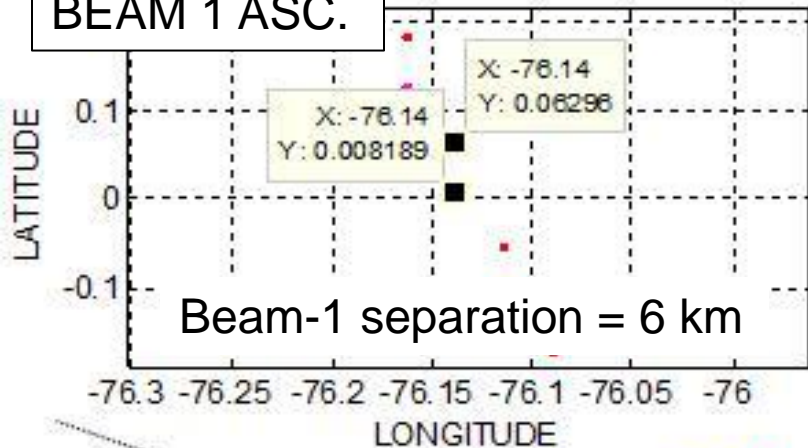


# Beam Compass Azimuth Angle for Descending Flight

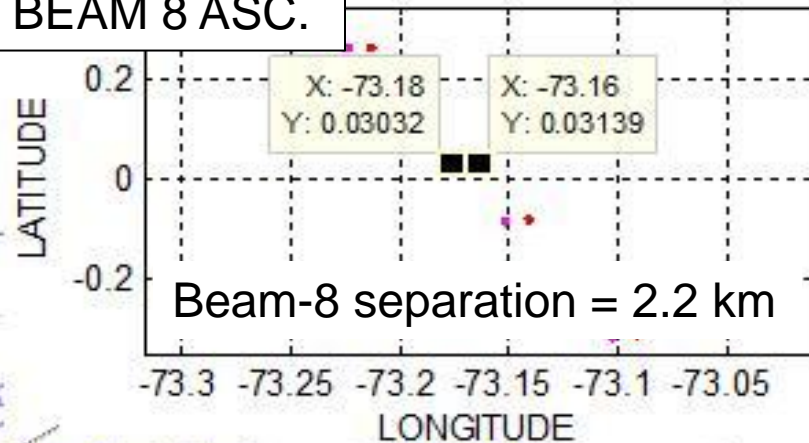


$$\text{Beam\_CAA\_Yaw} = \text{modulo} ((\text{SV\_CAA} + \text{Beam\_Az} + \text{Yaw}), 360)$$

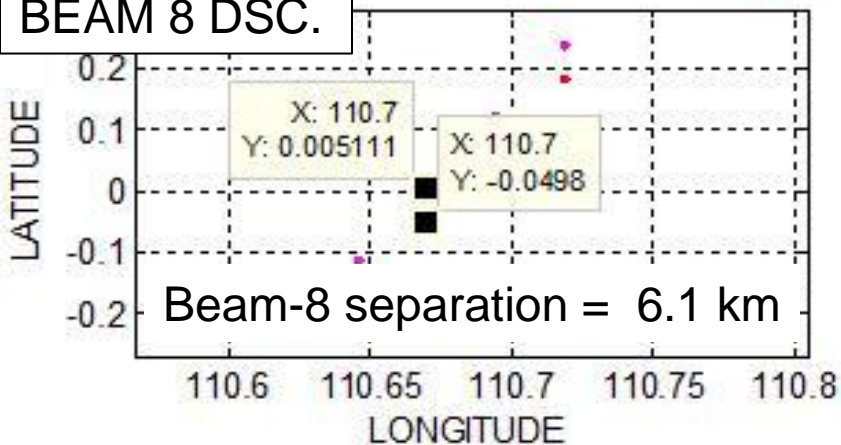
BEAM 1 ASC.



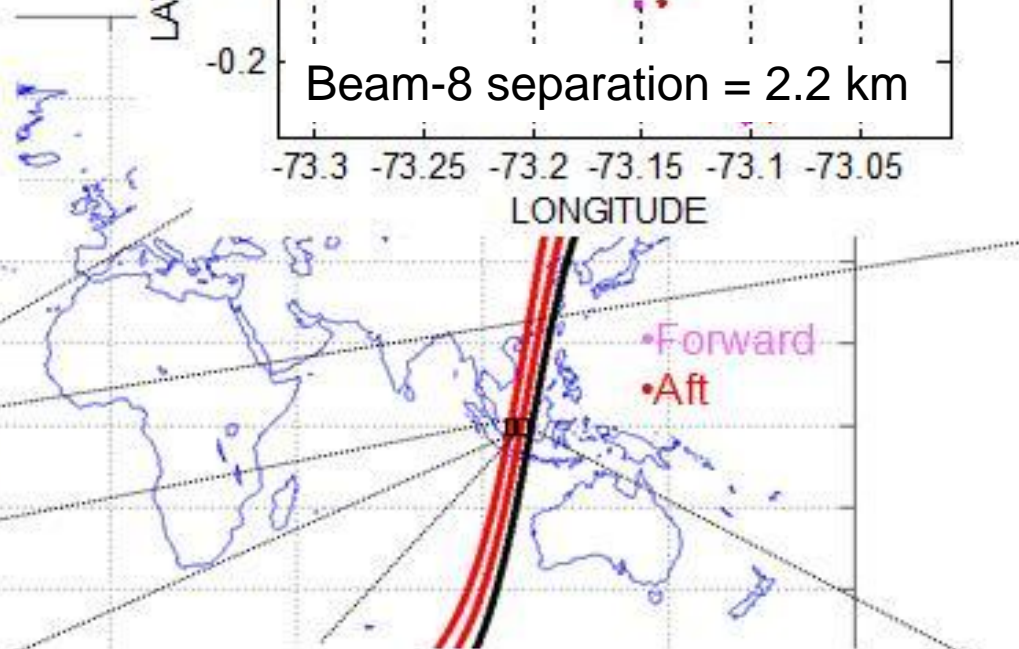
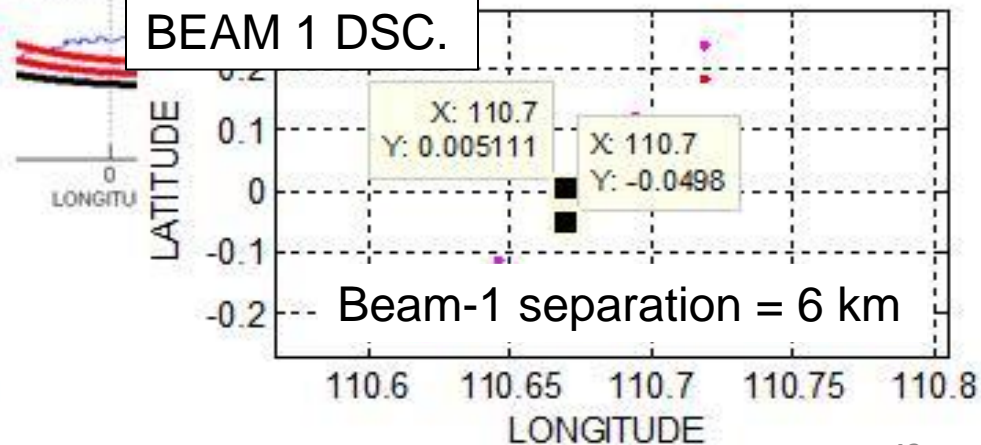
BEAM 8 ASC.



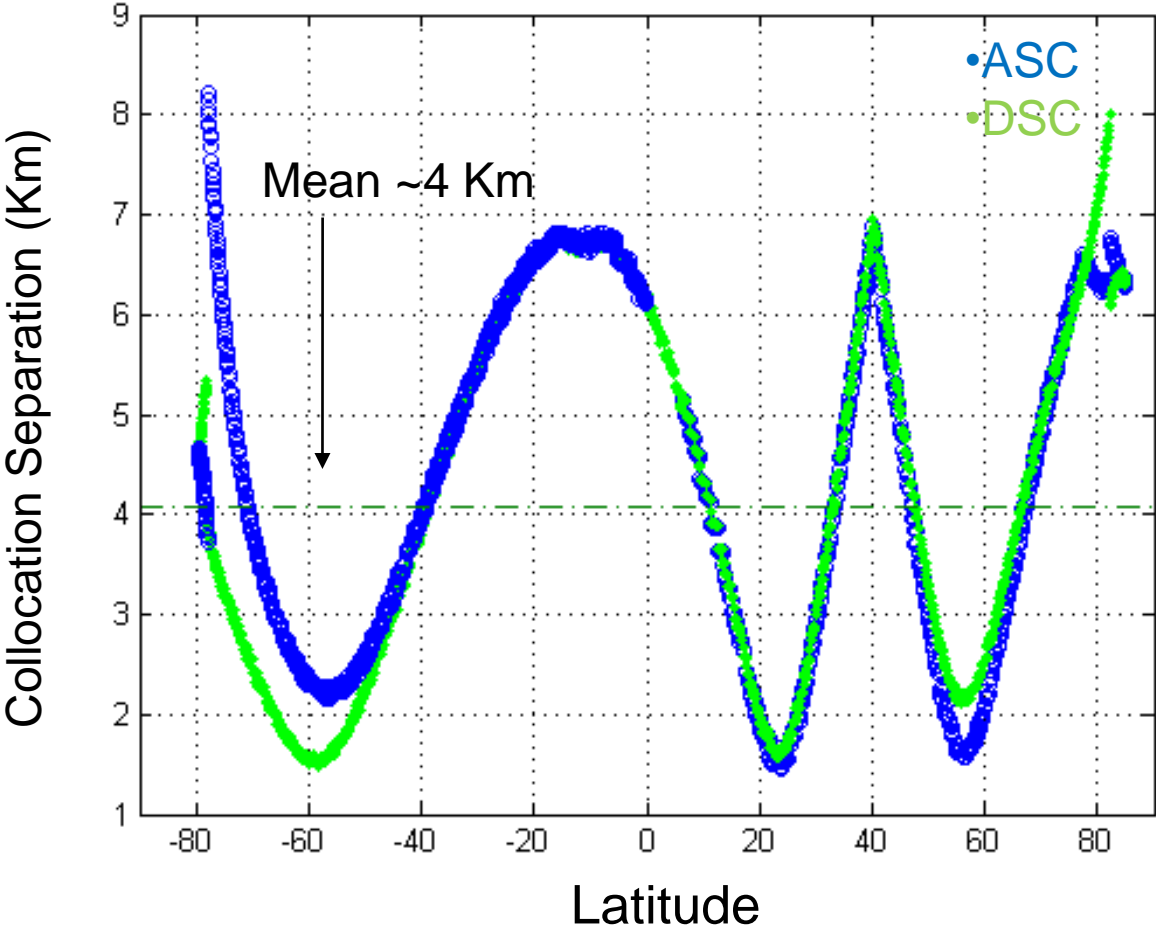
BEAM 8 DSC.



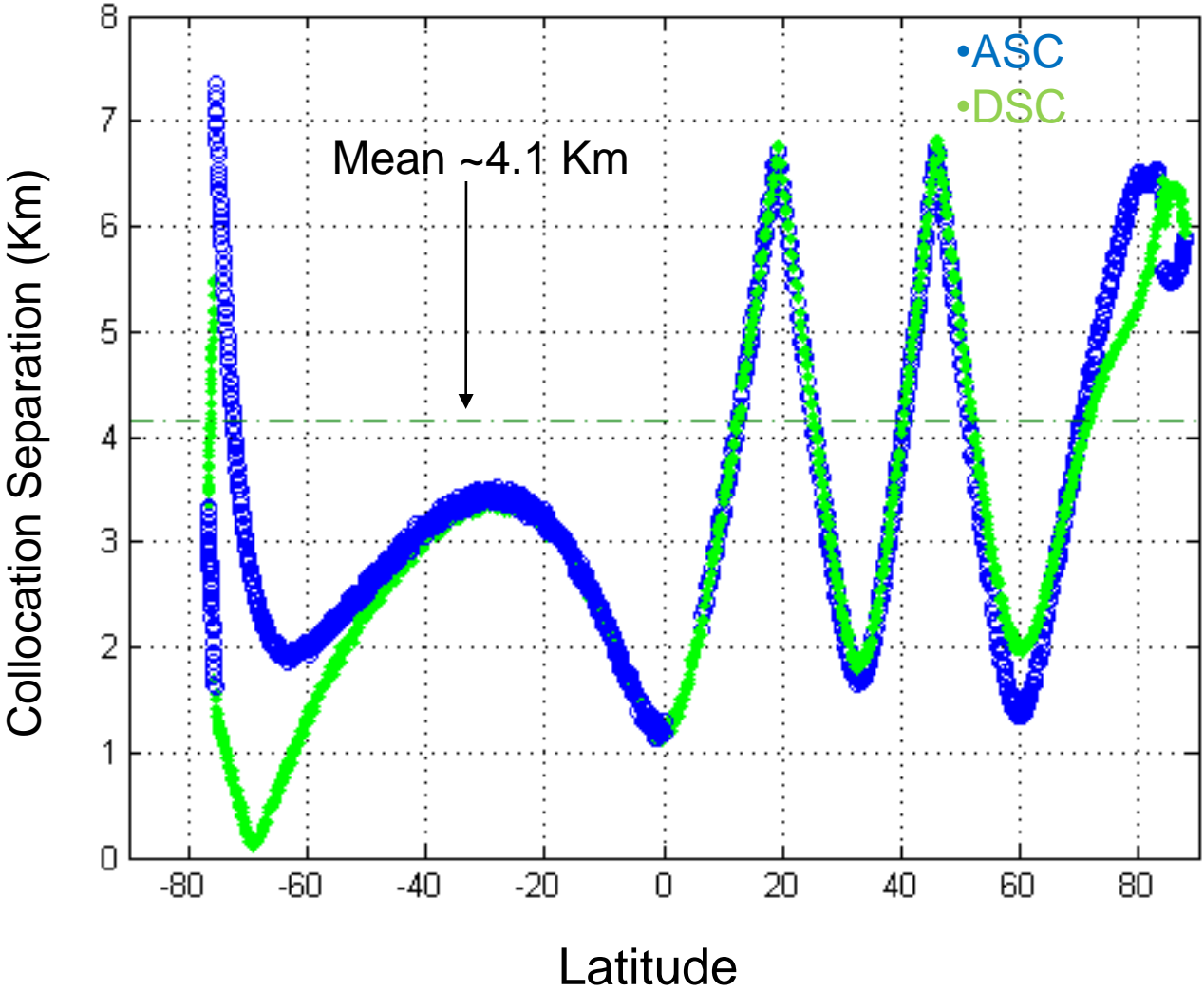
BEAM 1 DSC.



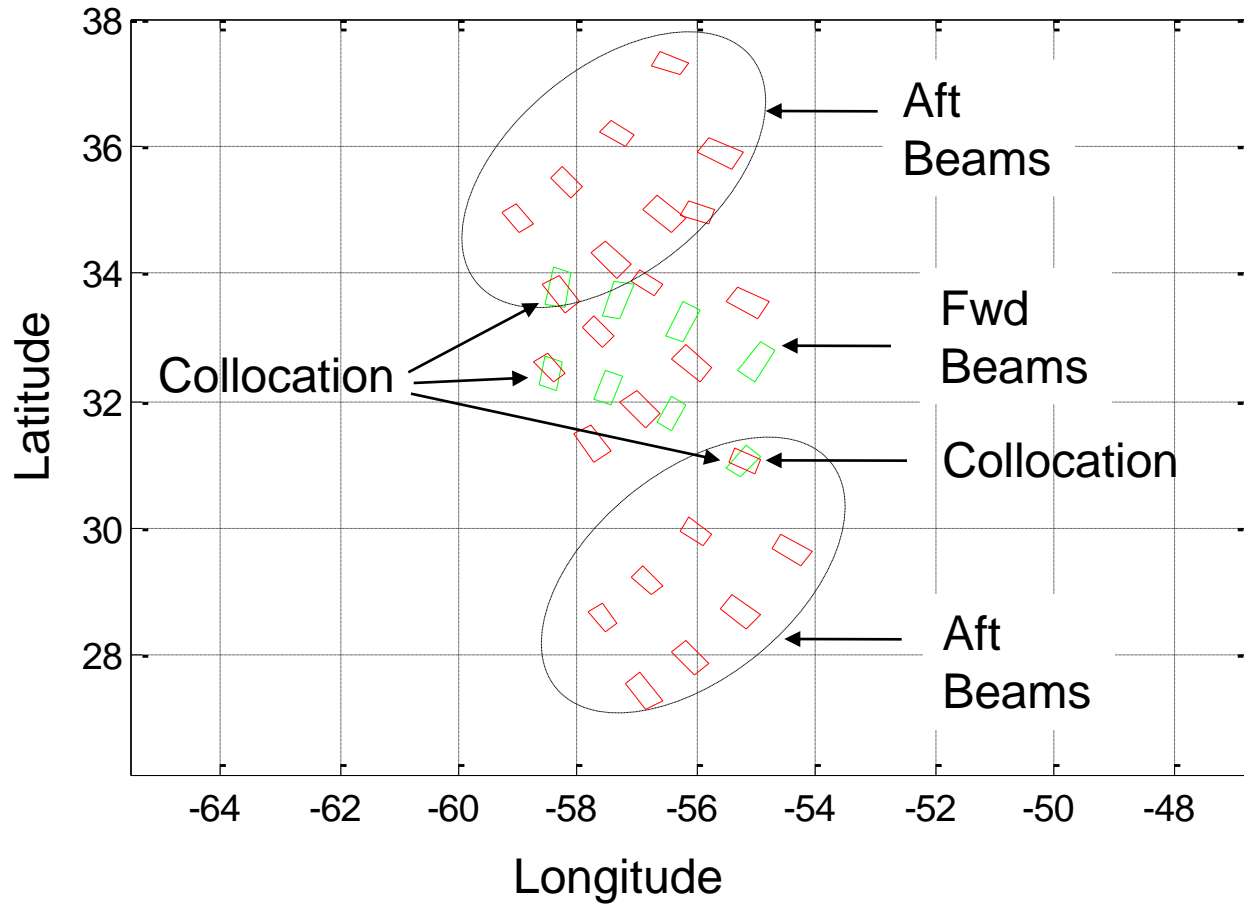
# Forward/Aft Beam-1 Collocation Separation



# Forward/Aft Beam-8 Collocation Separation

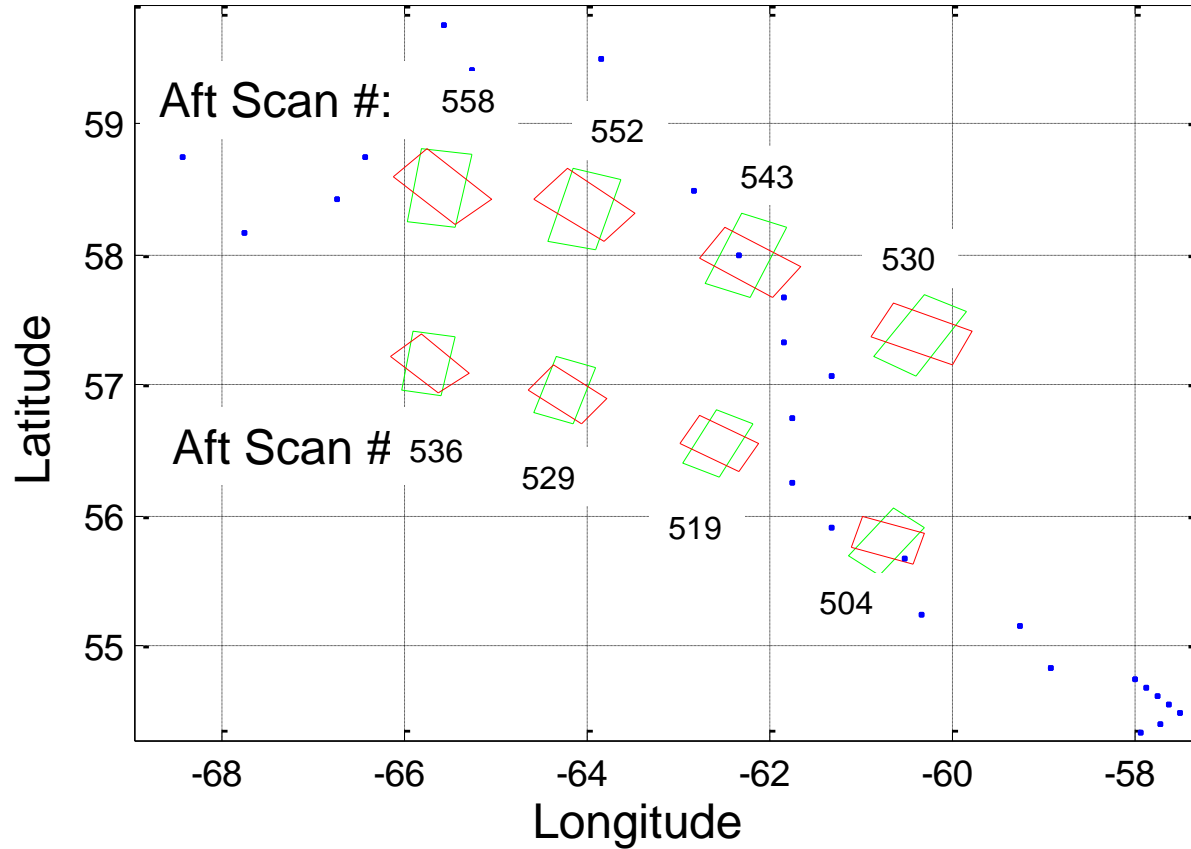


# A Snapshot of 3 Forward Beams Collocating



# All Forward Beams Collocating with Different Aft Scans

Fwd Scan # 437



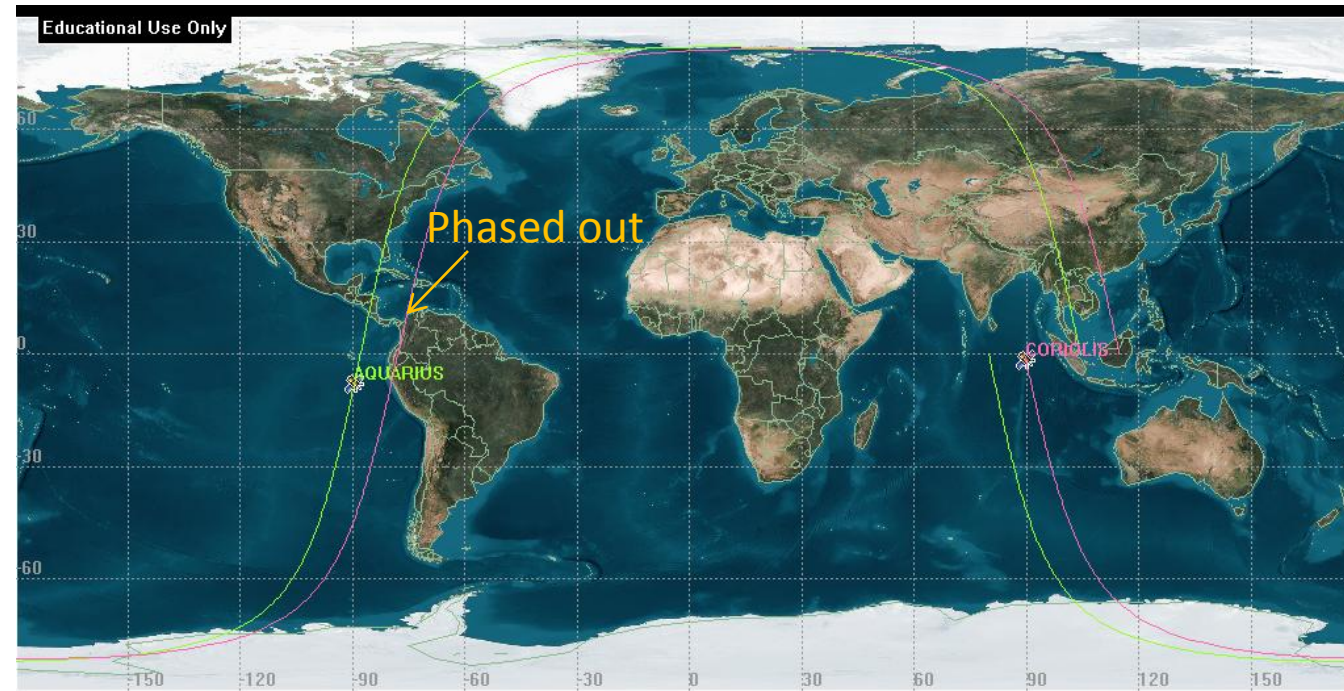
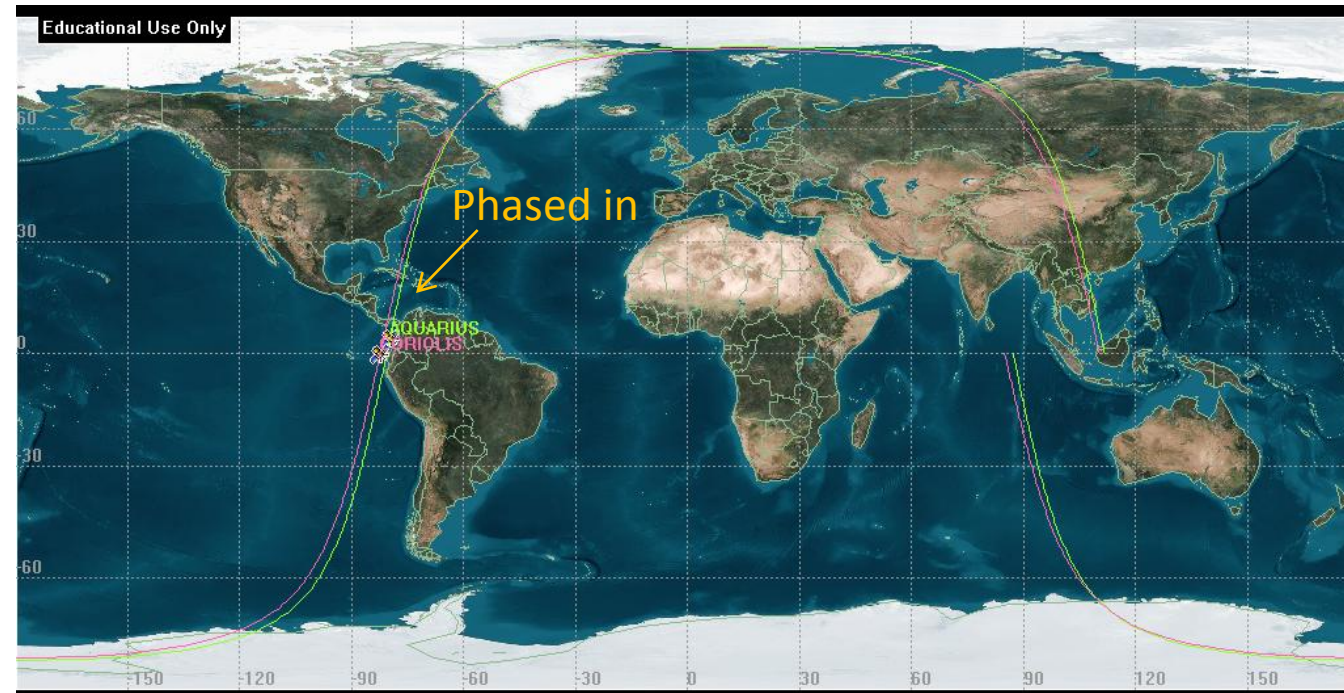
# Post-launch Inter-Satellite Radiometric Calibration using WindSat



# WindSat shares similarities in orbit (ground track), radiometer frequencies and swath overlap with MWR

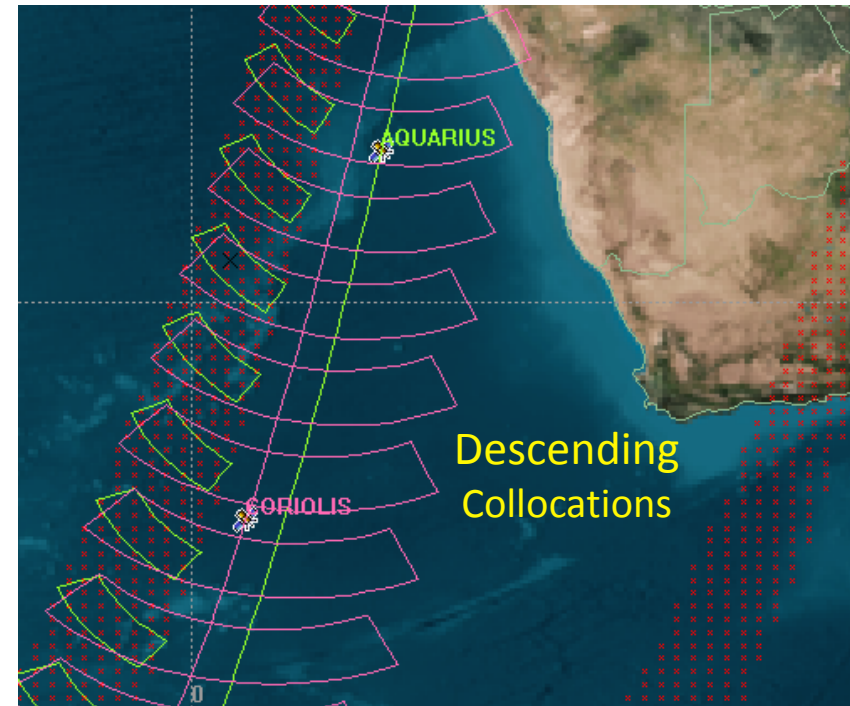
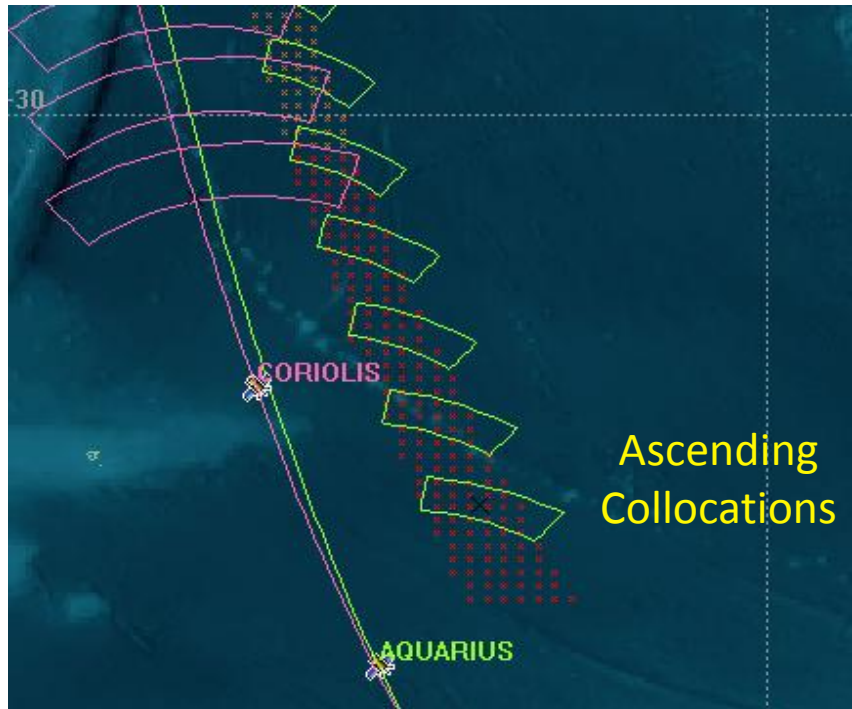
Parameter	WindSat	MWR
Altitude	840 Km	657 Km
Eccentricity	0.00134	0.0012
Inclination Angle	98.7°	98.01°
Ascending Node	6 p.m.	6 p.m.
Frequency	23.8 (V & H) and 37.0 (V & H)	23.8 (V) and 36.5 (V & H) GHz
Swath Width	~950 Km	~380 Km
Earth Incidence Angle	53°	52° & 58°





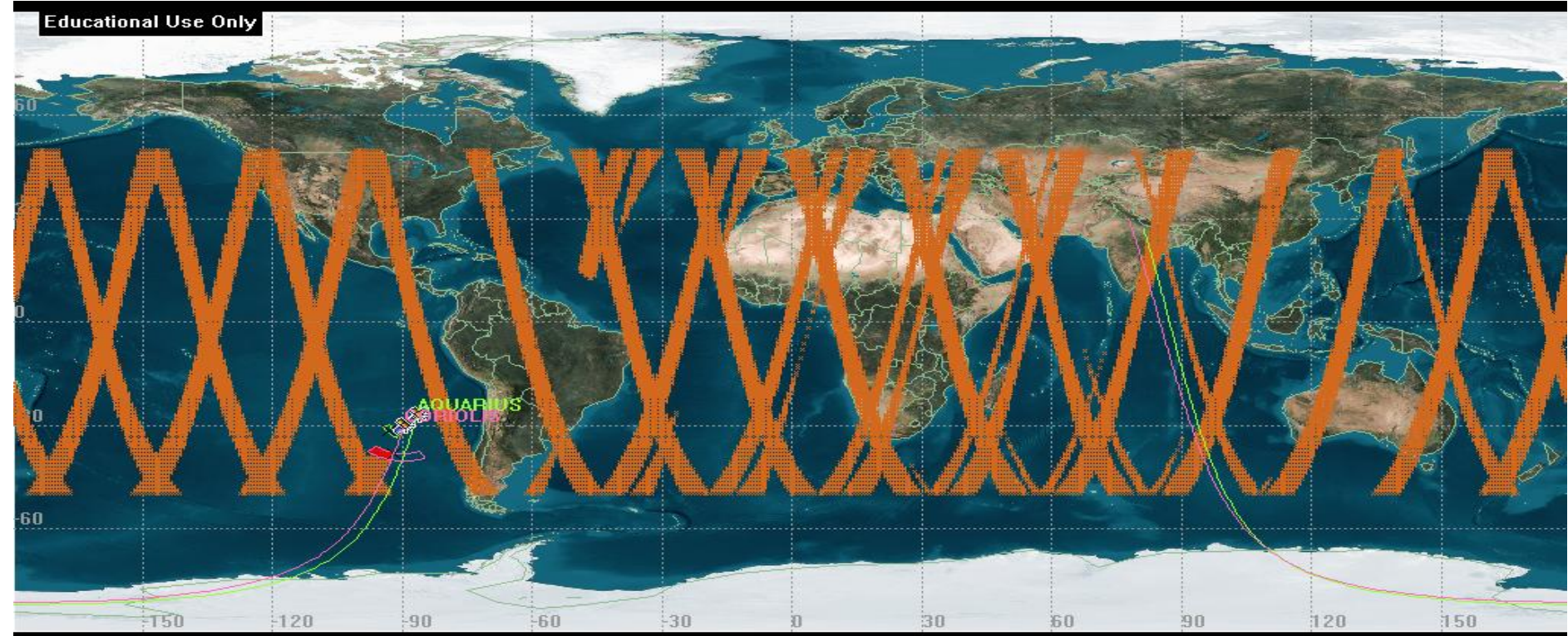
- Aquarius speed > Coriolis & it laps in ~45 hours and 36 mins
- During half of this period, satellite ground tracks are out of phase
- Time for satellite ground tracks to be coincident (in phase at same Lat/Lng) is ~57 days

# ASC/DSC Collocations (0.5° resolution)





Educational Use Only



- Approx 19,000 collocations in 45 hrs ( $\pm 50^\circ$  Lat)
  - $(0.5^\circ \times 0.5^\circ)$  &  $\pm 45$  min window
- Approx 1 Million ocean collocations in 5 months

# Conclusions

- The MWR  $T_b$  simulation is validated to have radiometric and temporal/spatial accuracy
- CONAE's yaw steering technique to collocate the forward & aft MWR beams has also been verified with a mean collocation separation  $\sim 4$  Km
- The inter-satellite swath collocation between WindSat and MWR shows that  $\sim 5$  months in orbit, there will be  $\sim 1$  Million ocean collocations

# Future Work

- A four month simulated  $T_b$  dataset for the 3-channel MWR will be delivered to CONAE for the pre-launch geophysical retrieval algorithms development
- The MWR retrievals will be validated through near simultaneous, collocated comparisons with WindSat's Environmental Data Records (EDRs)

# Backup Slides



## Satellite/Sensor Geometry - Incidence Plane [cont]

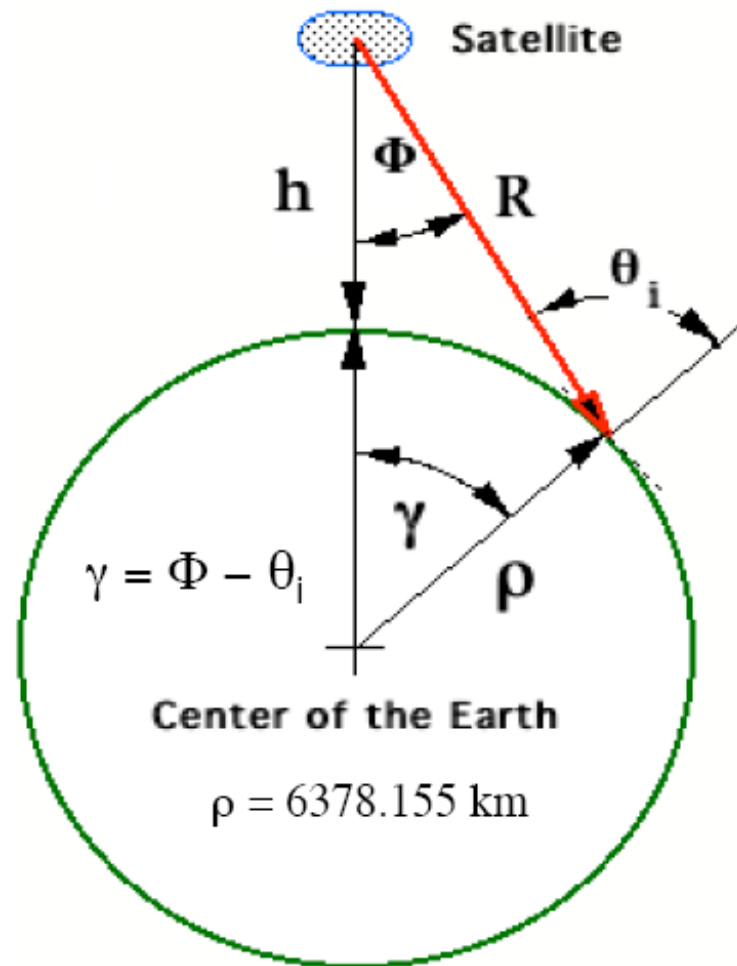
NADIR/INCIDENCE ANGLE RELATIONSHIPS

Nadir angle  $\Phi = A \text{ SIN} \left[ \frac{\rho}{\rho + h} \text{ SIN} \theta_i \right]$

Incidence Angle  $\theta_i = A \text{ SIN} \left[ \frac{\rho + h}{\rho} \text{ SIN} \Phi \right]$

SLANT RANGE

$$R = \frac{\rho \text{ SIN} \gamma}{\text{SIN} \Phi}$$

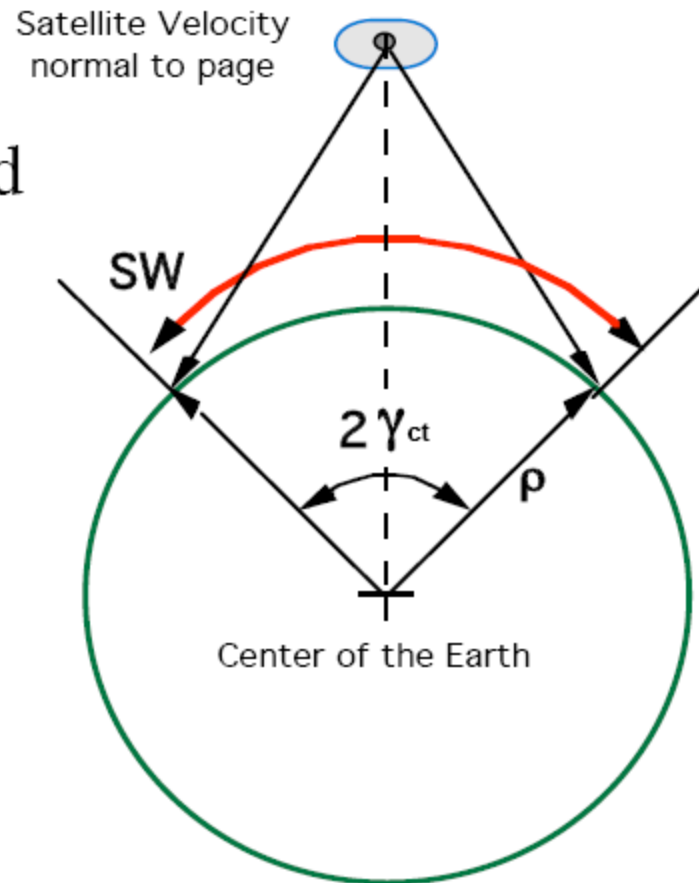


# Satellite/Sensor Geometry - Across-Track Plane

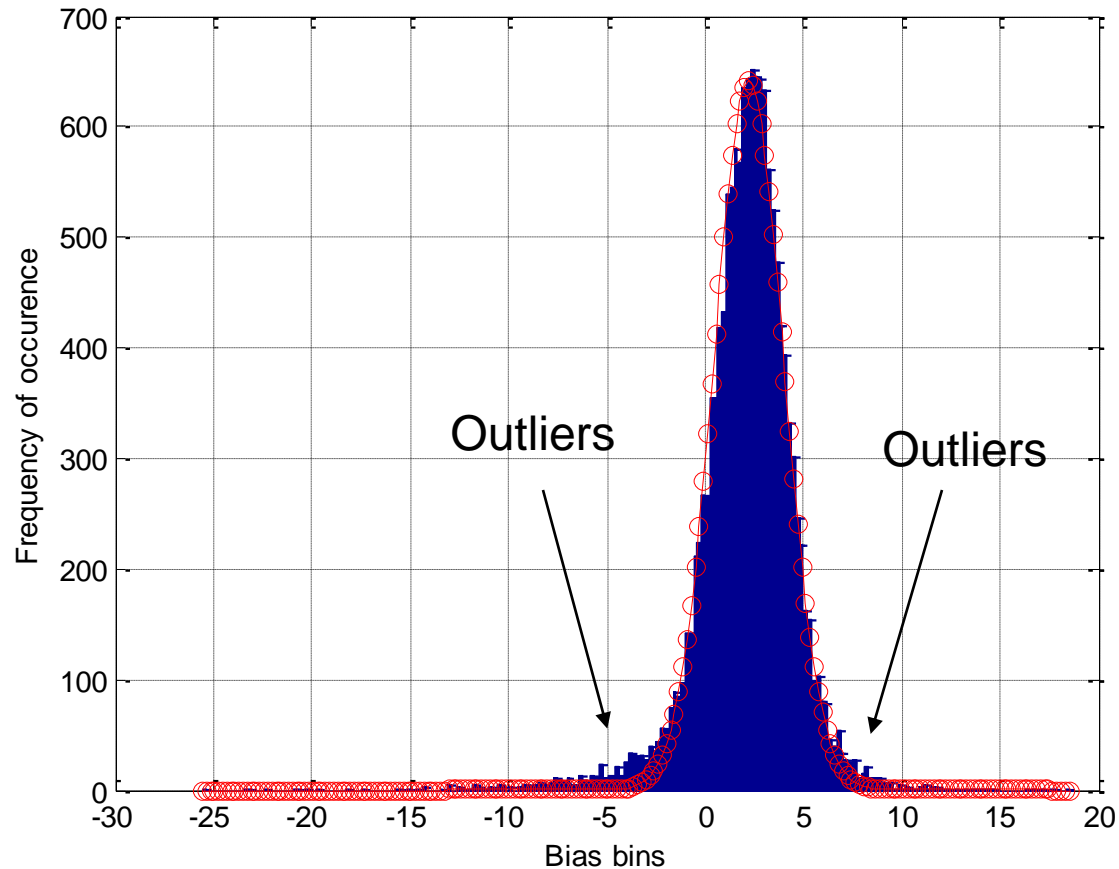
Swath Width is measured in the cross-track plane along the surface of the earth

$$SW = 2 \gamma_{ct} \rho$$

Note:  $\gamma_{ct}$  is in units of radians



# Best-Fit Gaussian



Gaussian fit for Bin # 5 of Wind Speed Bias